

InSb Nanoflags SQUIDs

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Genova, 2024 12 16



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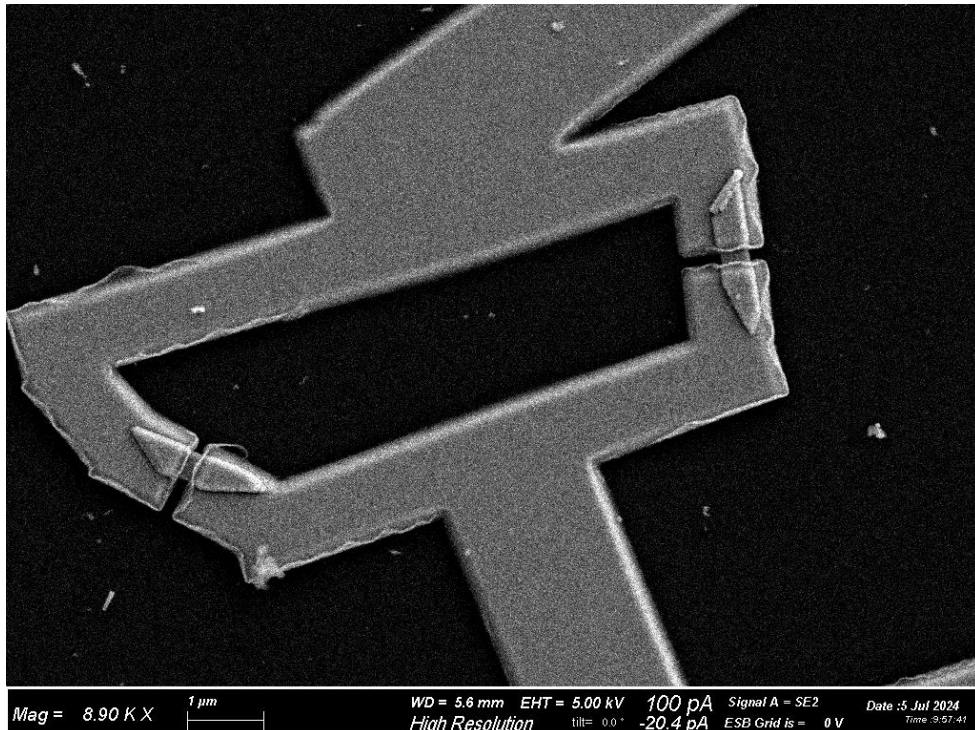
Outline

- Two Josephson Junctions in parallel
 - Conductance of a single Josephson Junction
 - Conductance of a SQUID
- Interference
 - Symmetric SQUID
 - Asymmetric SQUID

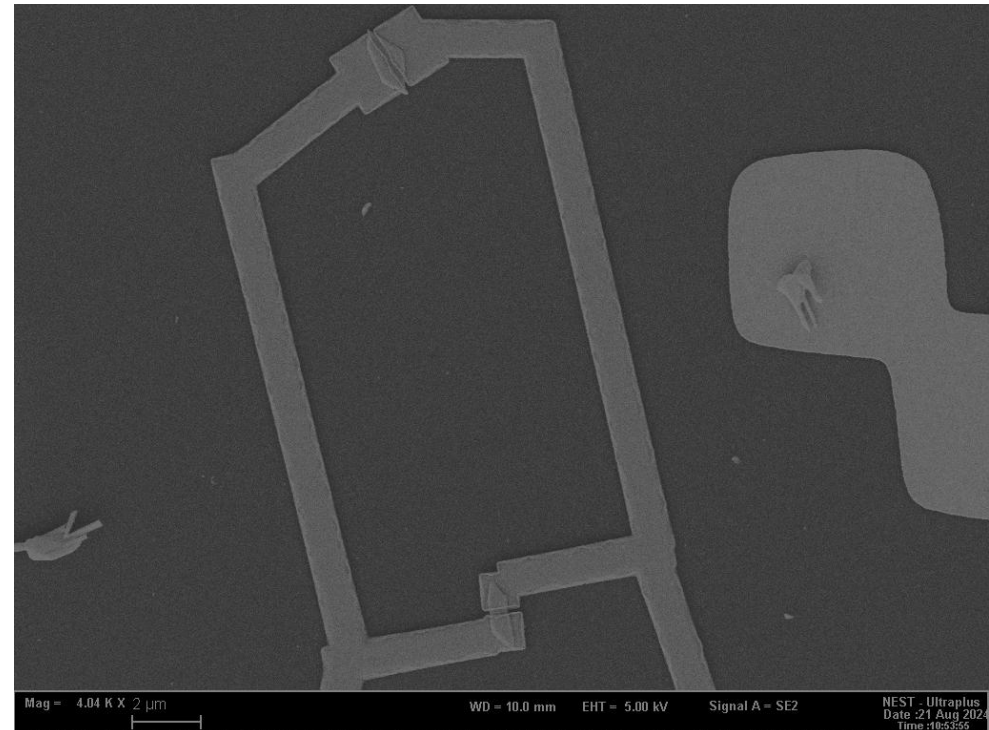
Two Josephson Junctions in parallel

Devices: Symmetric and Asymmetric SQUIDs

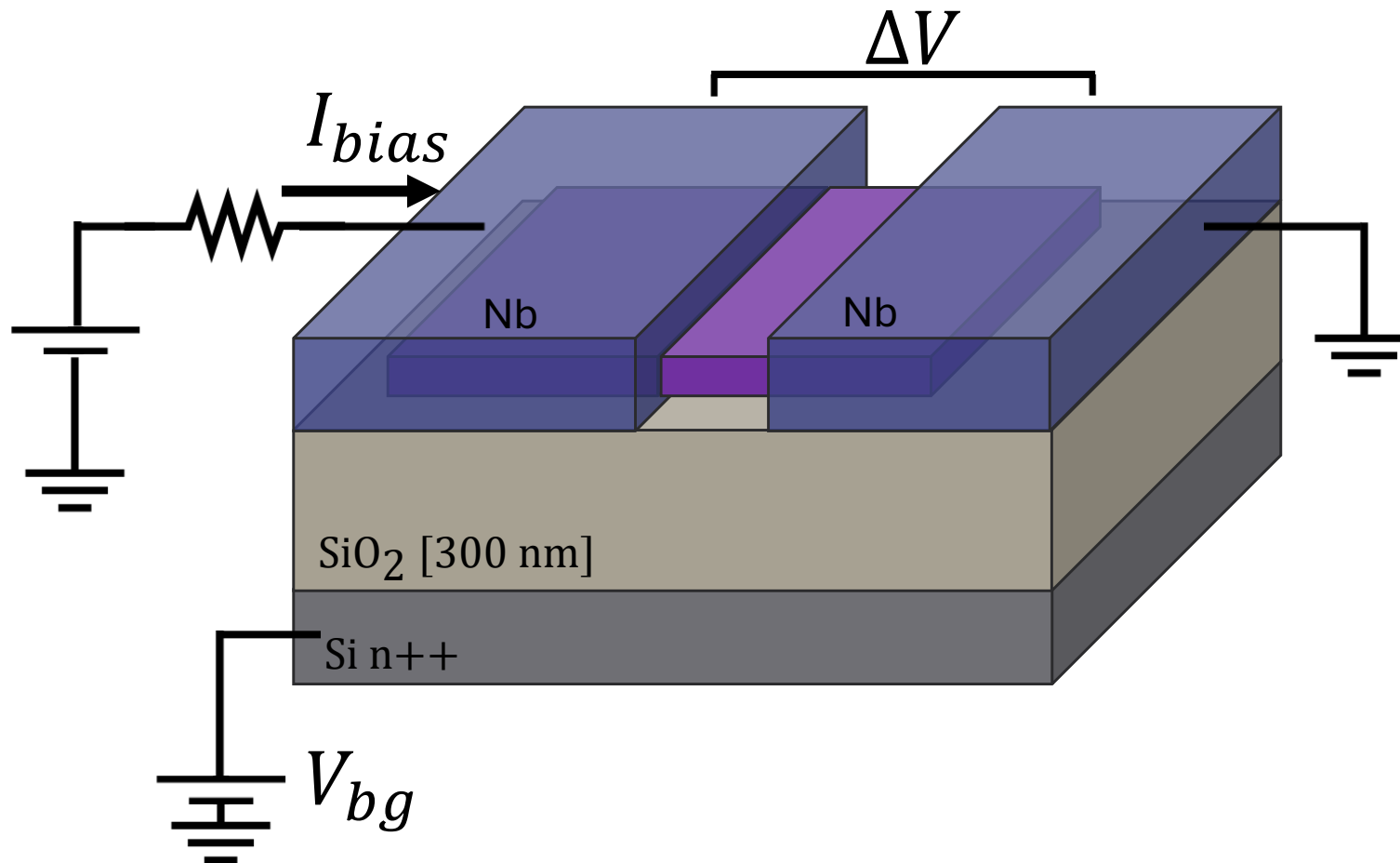
Symmetric SQUID



Asymmetric SQUID



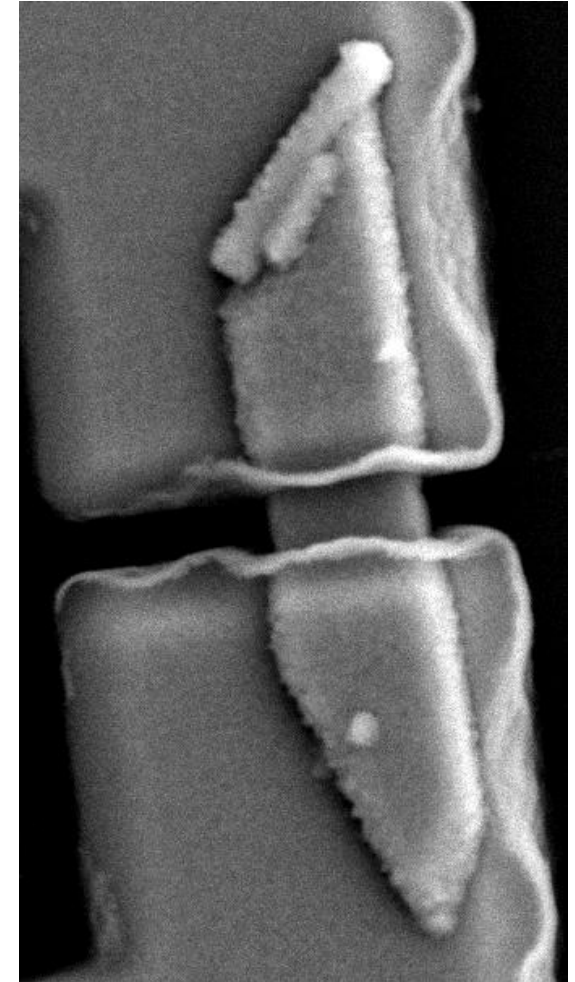
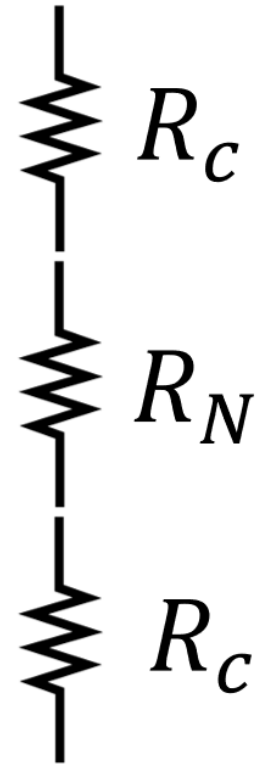
Measurement Mode: Current Bias



- Contact resistance R_c must be included in the conductance model

Single Josephson Junction

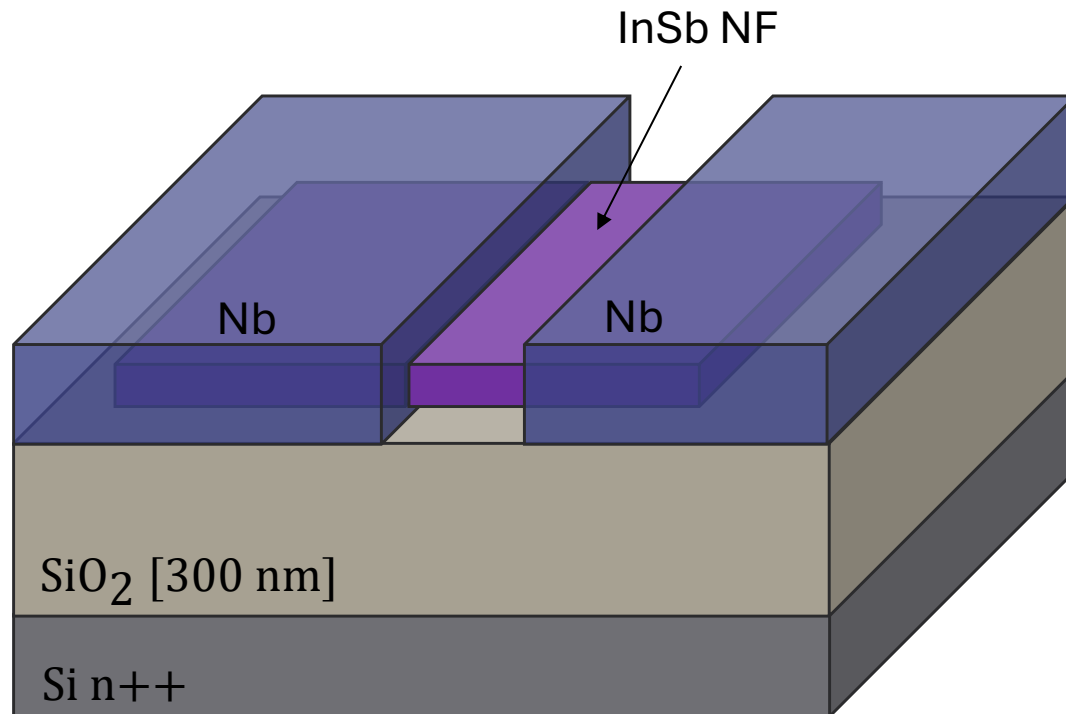
$$\frac{1}{G_{JJ}} = R_c + R_N + R_c$$



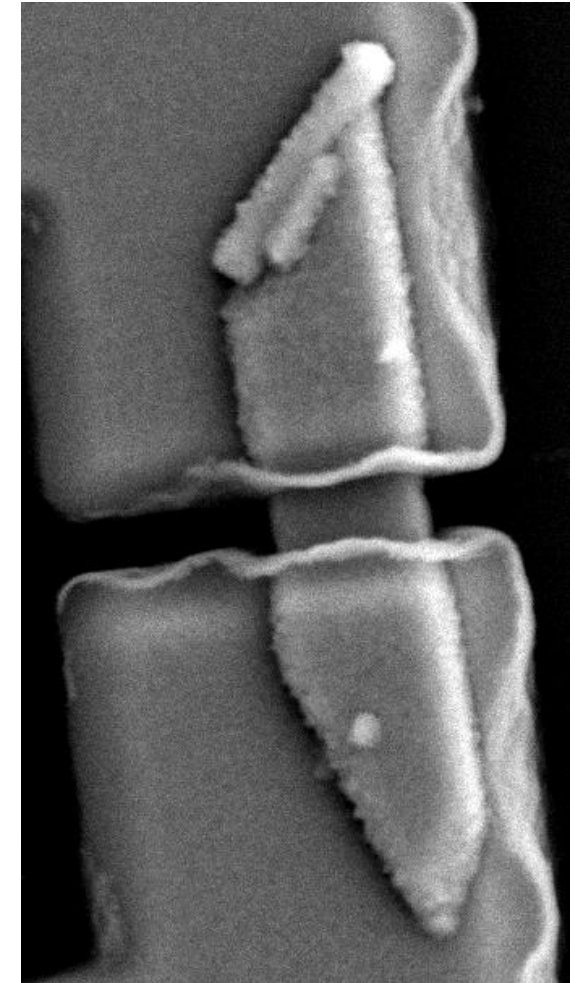
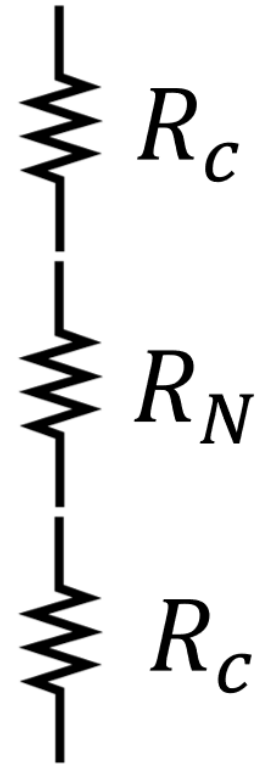
JJ of SQUID3 – C2S4

Single Josephson Junction

$$R_N = \left(c_{ox} \frac{W}{L} \mu (V_{bg} - V_{th}) \right)^{-1}$$



$$\begin{aligned} L &= 200 \text{ nm} \\ W &= 380 \text{ nm} \\ c_{ox} &= 1.15 \cdot 10^{-8} \text{ F cm}^{-2} \end{aligned}$$

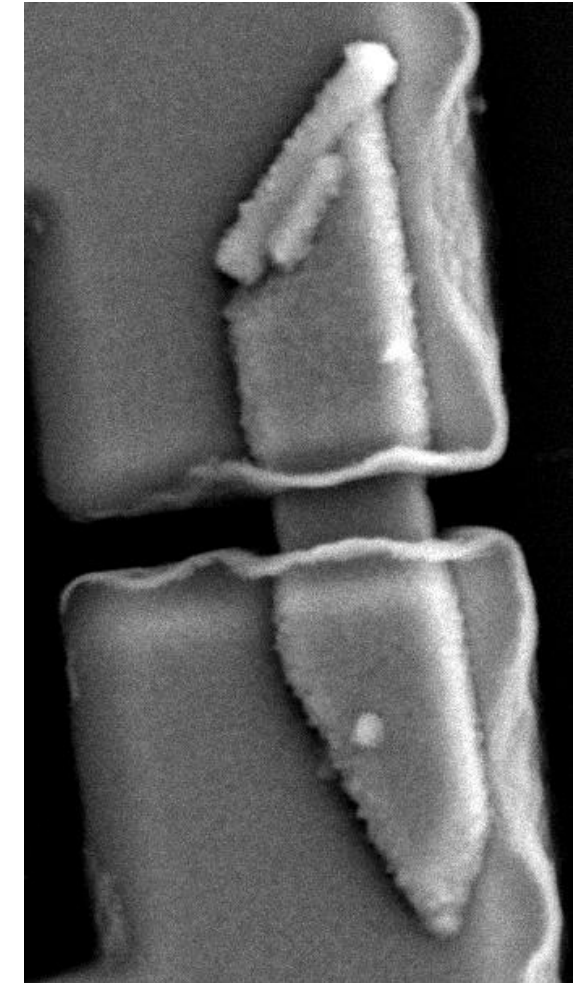
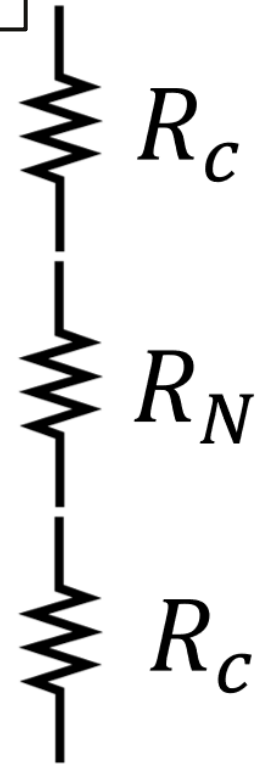
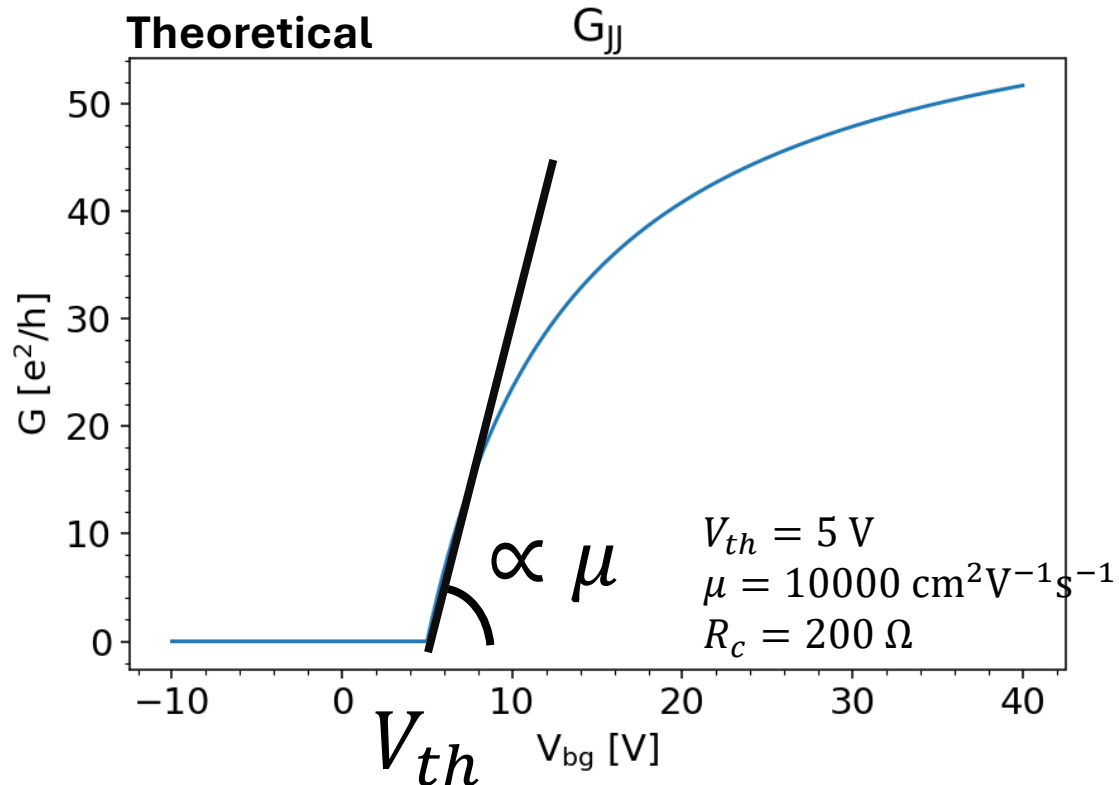


JJ of SQUID3 – C2S4

Single Josephson Junction

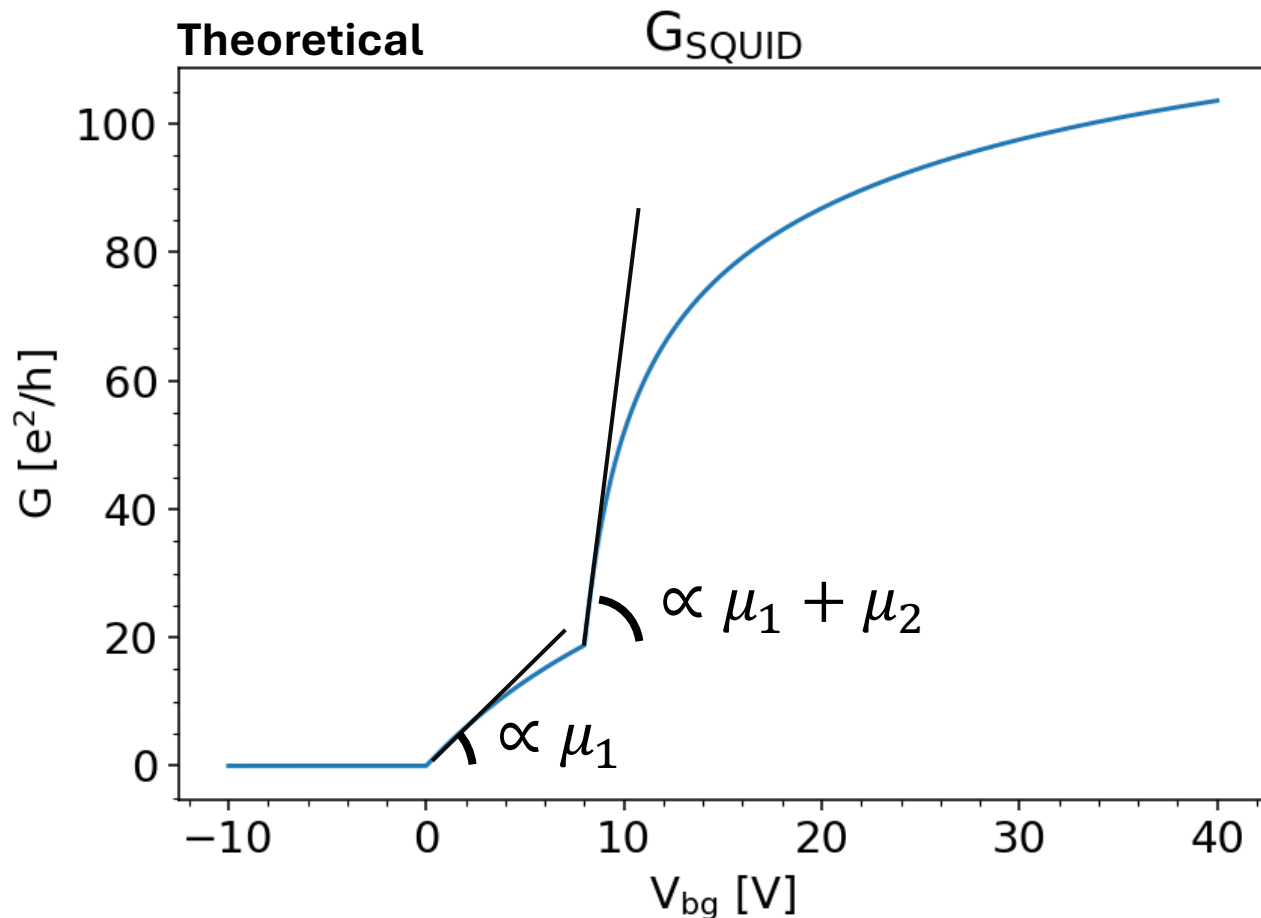
$L = 200 \text{ nm}$
 $W = 380 \text{ nm}$
 $c_{ox} = 1.15 \cdot 10^{-8} \text{ F cm}^{-2}$

$$\frac{1}{G_{JJ}} = 2R_c + \left(c_{ox} \frac{W}{L} \mu (V_{bg} - V_{th}) \right)^{-1}$$



JJ of SQUID3 – C2S4

Conductance model of a SQUID



$$G_{SQUID} = G_{JJ,1} + G_{JJ,2}$$

$$V_{th1} = 0 \text{ V},$$

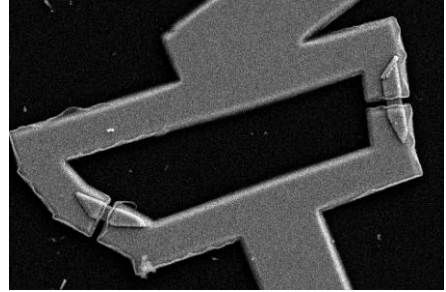
$$\mu_1 = 4000 \text{ cm}^2 \text{V}^{-1} \text{s}^{-1}$$

$$V_{th2} = 8 \text{ V}$$

$$\mu_2 = 10000 \text{ cm}^2 \text{V}^{-1} \text{s}^{-1}$$

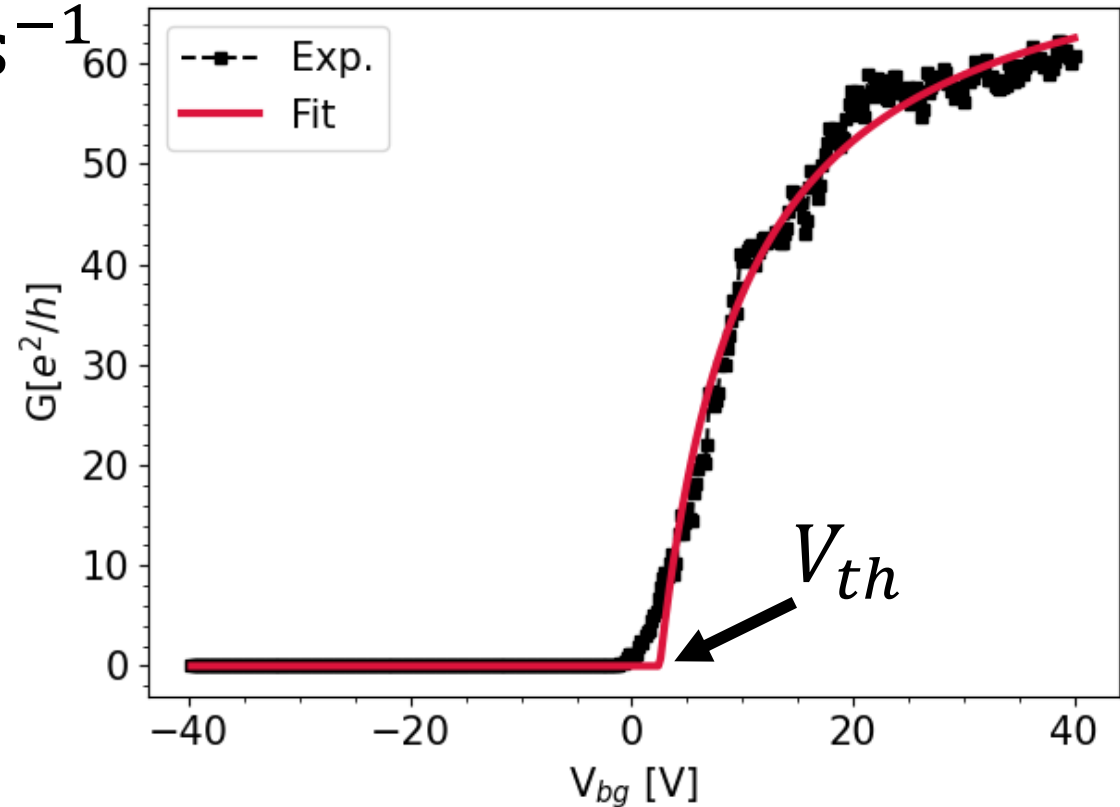
$$R_c = 200 \text{ } \Omega$$

Symmetric SQUID conductance

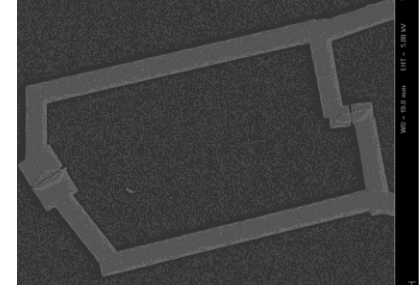


- $V_{th} = 2.5 \pm 0.1 \text{ V}$
- $\mu = 8200 \pm 200 \text{ cm}^2\text{V}^{-1}\text{s}^{-1}$
- $R_c = 342 \pm 3 \Omega$

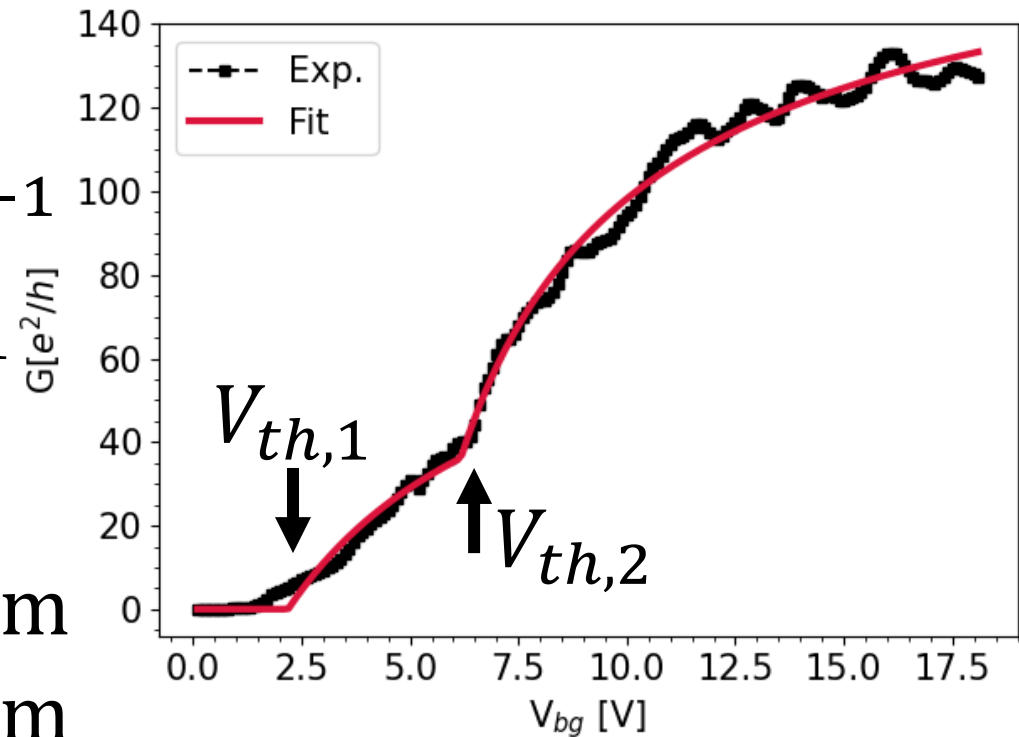
$$l_{MFP} = \frac{\hbar\mu}{e} \sqrt{2\pi n_{2d}} = 150 \text{ nm @ BG} = 20 \text{ V}$$



Asymmetric SQUID conductance



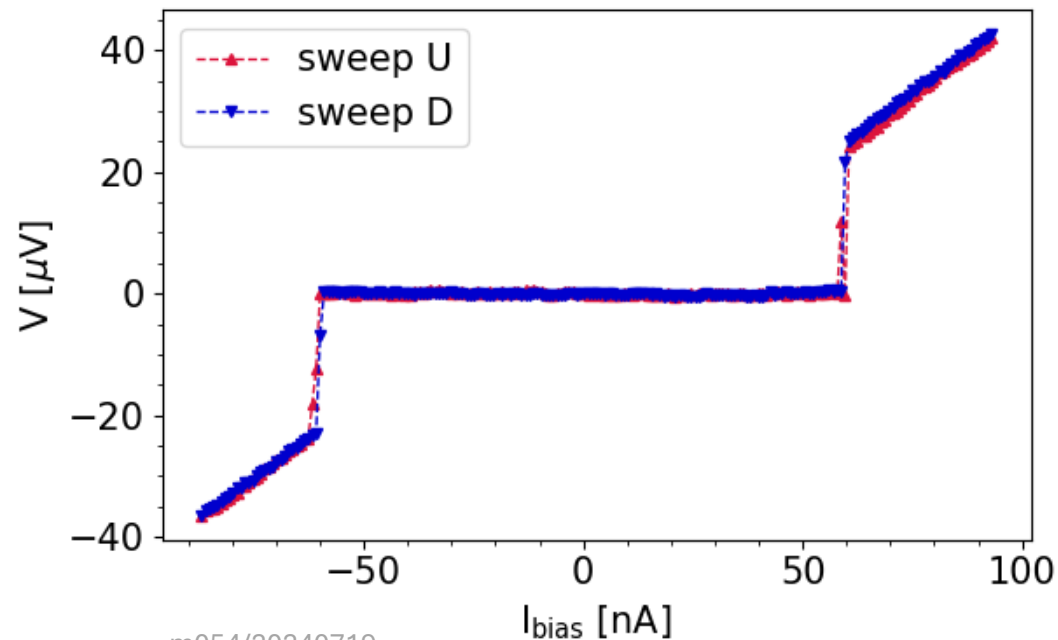
- $V_{th,1} = 2.2 \pm 0.1 \text{ V}$
- $V_{th,2} = 6.2 \pm 0.1 \text{ V}$
- $\mu_1 = 18600 \pm 950 \text{ cm}^2\text{V}^{-1}\text{s}^{-1}$
- $\mu_2 = 9700 \pm 500 \text{ cm}^2\text{V}^{-1}\text{s}^{-1}$
- $R_c = 147 \pm 2 \Omega$
- At $V_{bg} = 15 \text{ V}$ $l_{MFP,1} = 300 \text{ nm}$
 $l_{MFP,2} = 140 \text{ nm}$



VI traces @ $T = 350$ mK

Symmetric SQUID

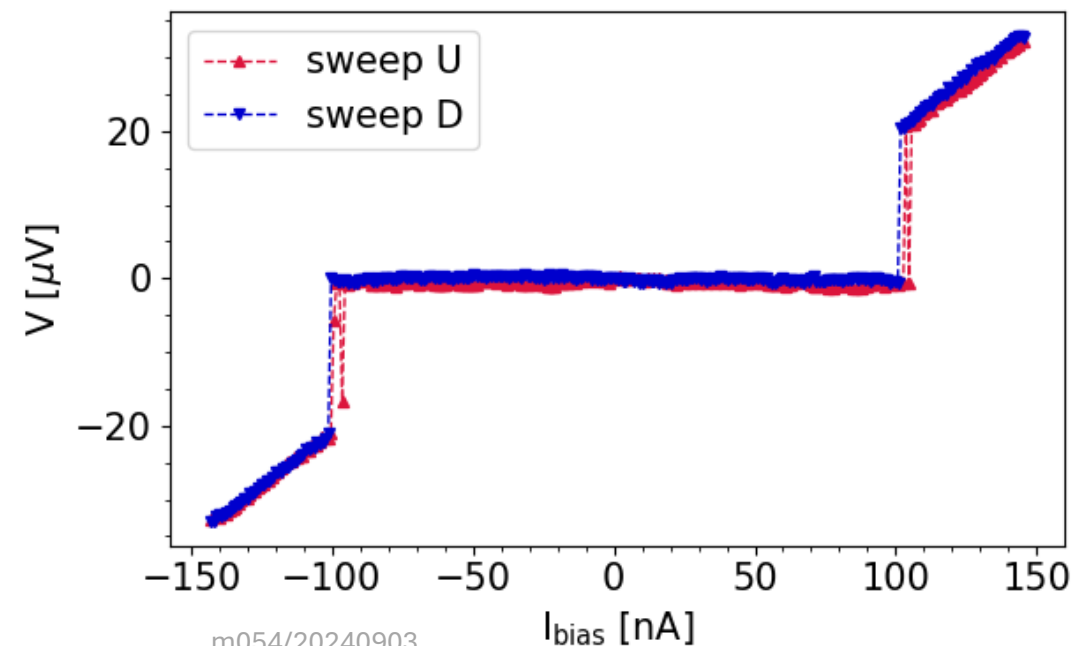
$$V_{BG} = 20.0 \text{ V} \quad I_{sw} \cong 60 \text{ nA}$$



m054/20240719

Asymmetric SQUID

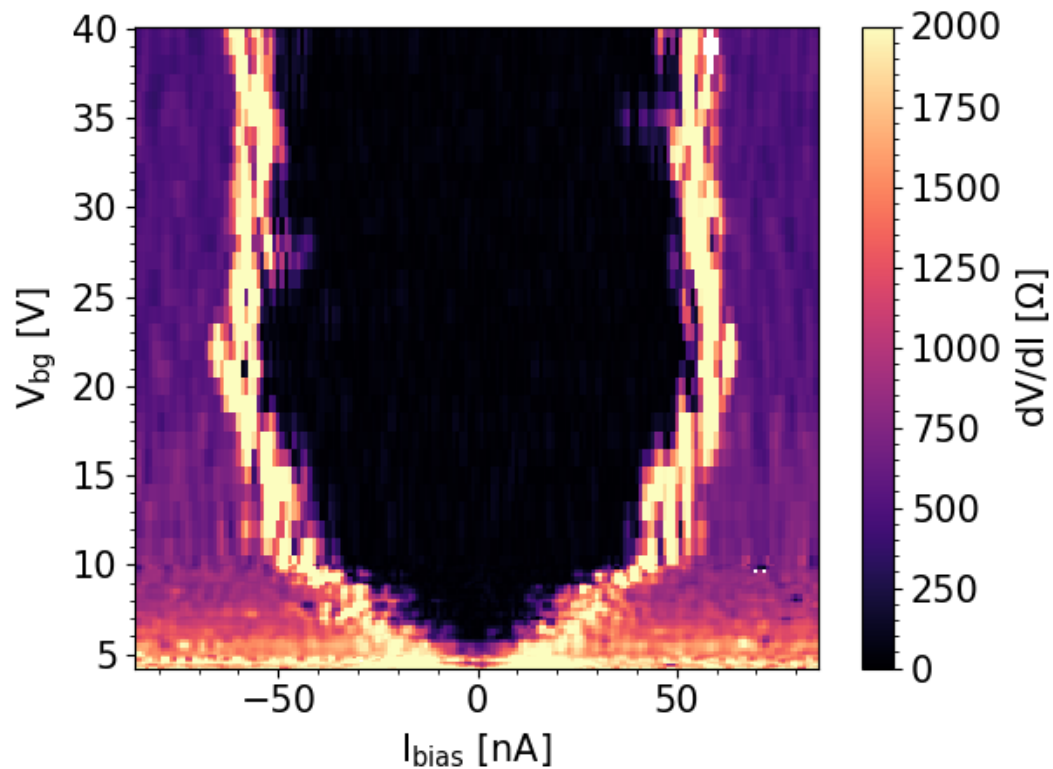
$$V_{BG} = 18.0 \text{ V} \quad I_{sw} \cong 100 \text{ nA}$$



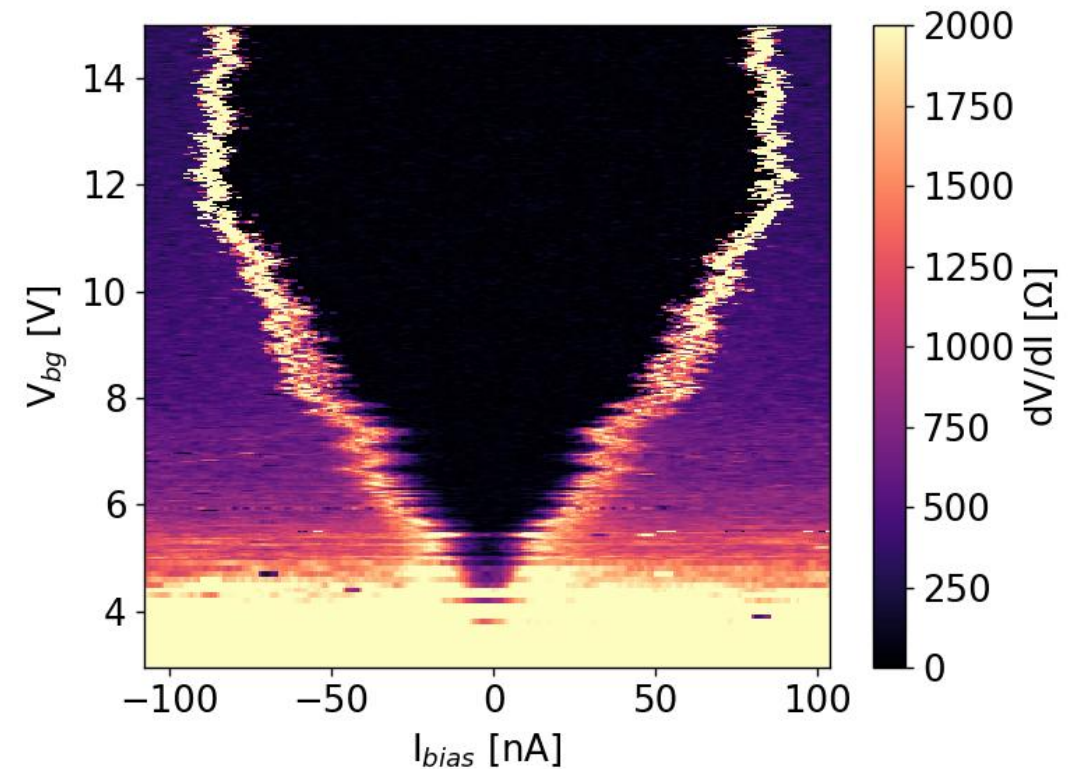
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Backgate control of supercurrent @ $T = 350$ mK

Symmetric SQUID



Asymmetric SQUID

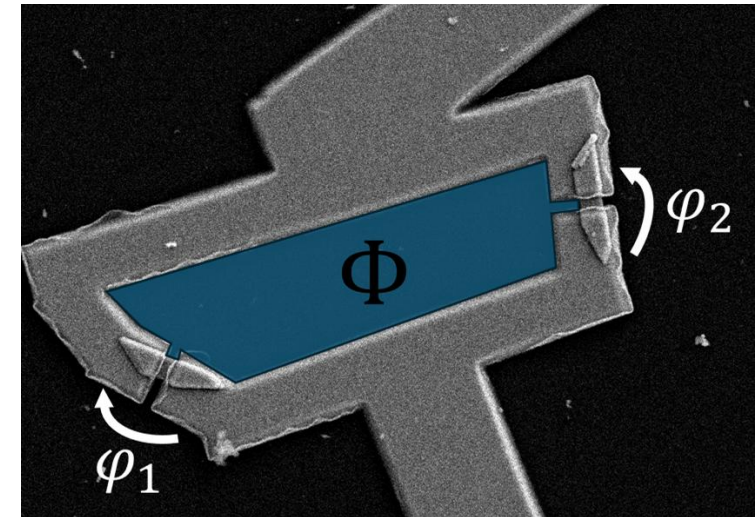


Interference on Symmetric SQUID

Basic Theory

- $I_{SQUID} = I_1(\varphi_1) + I_2(\varphi_2)$
- $\varphi_1 - \varphi_2 = \frac{2\pi\Phi}{\Phi_0} + 2\pi n$
- Interference properties depend on the relations $I_1(\varphi_1)$, $I_2(\varphi_2)$ (Current Phase Relationships, CPRs)

$$\Phi = \Phi_{ext} - LI_{circ}$$
$$L = L_{geo} + L_{kin}$$



Basic Theory for Sinusoidal CPR

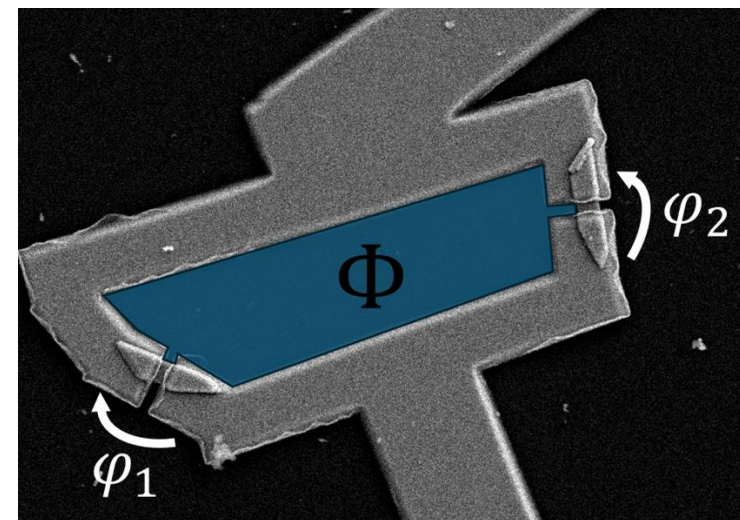
$$\bullet I_1(\varphi_1) = I_{c1} \sin(\varphi_1) \qquad I_2(\varphi_2) = I_{c2} \sin(\varphi_2)$$

$$\bullet I_c = \sqrt{(I_{c1} - I_{c2})^2 + 4I_{c1}I_{c2} \cos\left(\pi \frac{\Phi}{\Phi_0}\right)^2}$$

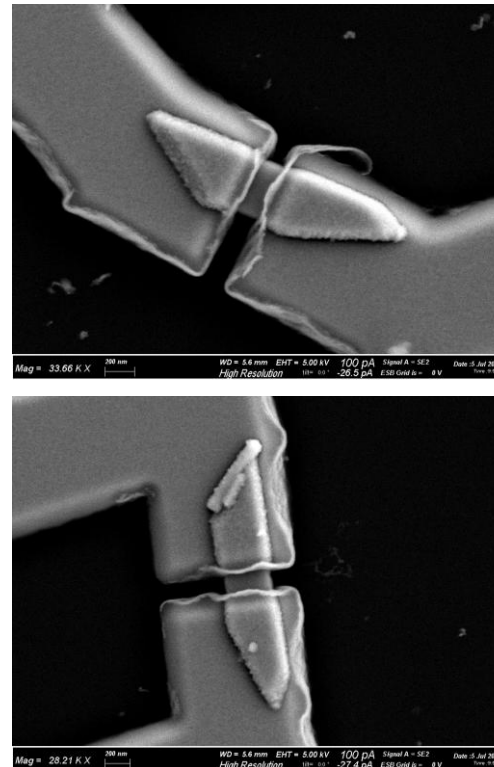
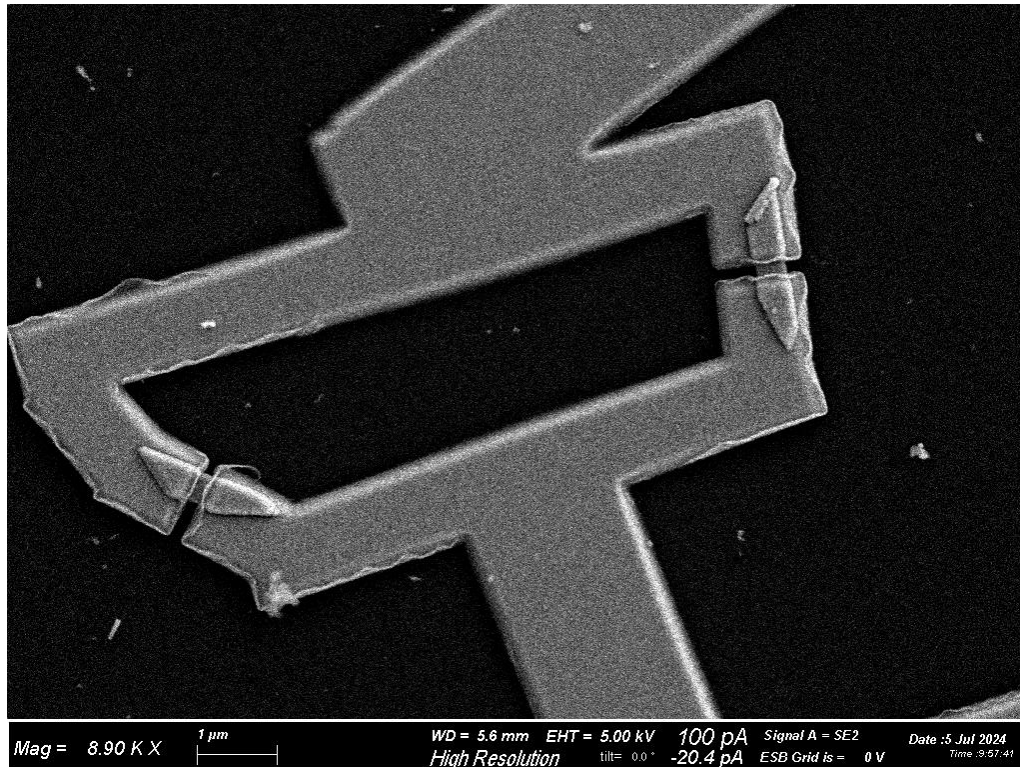
$$\begin{aligned} \Phi &= \Phi_{ext} - LI_{circ} \\ L &= L_{geo} + L_{kin} \end{aligned}$$

$$\Phi = n\Phi_0 \qquad \rightarrow I_c = |I_{c1} + I_{c2}|$$

$$\Phi = \Phi_0/2 + n\Phi_0 \rightarrow I_c = |I_{c1} - I_{c2}|$$



Symmetric SQUID: C2S4

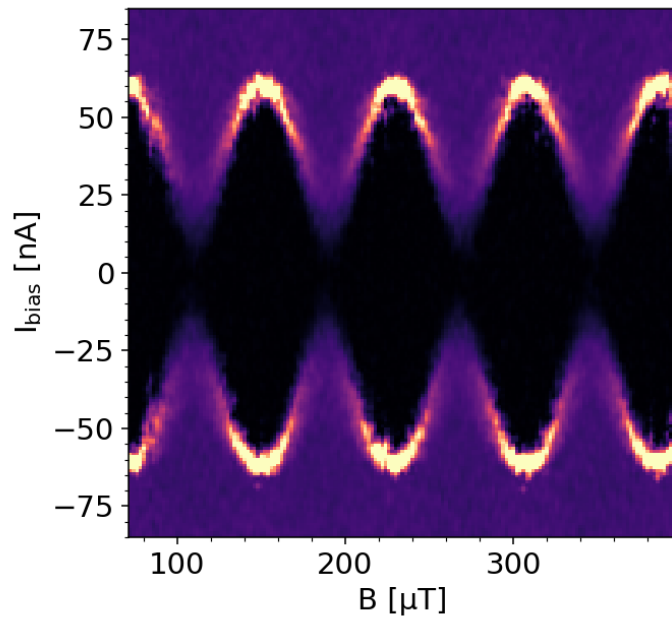


$$A_{geo} = 13.6 \mu\text{m}^2$$

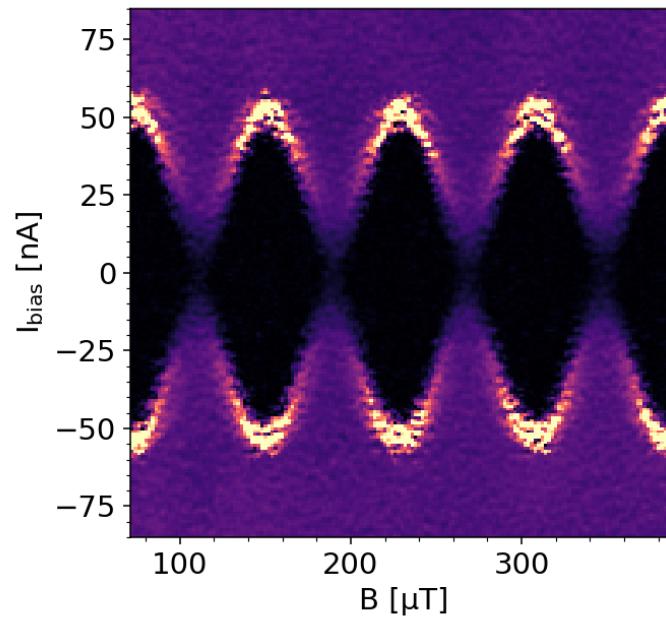
$$L_1 = 200 \text{ nm}$$
$$W_1 = 380 \text{ nm}$$

$$L_2 = 200 \text{ nm}$$
$$W_2 = 380 \text{ nm}$$

$$V_{BG} = 20.0 \text{ V}$$

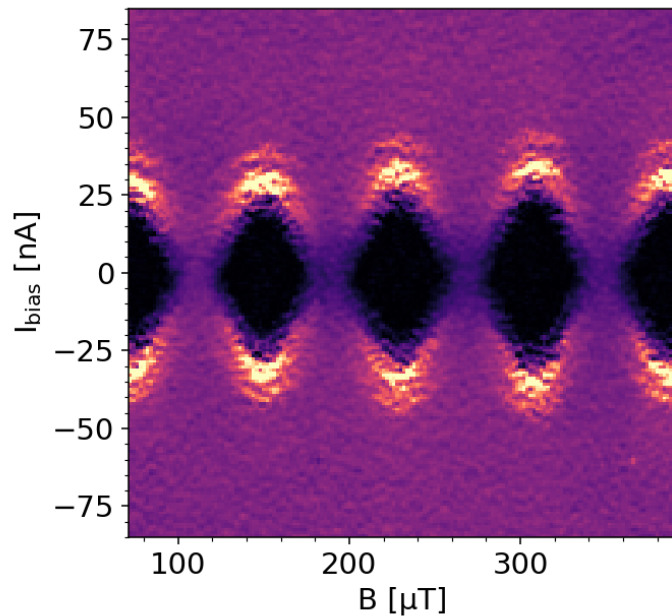


$$V_{BG} = 12.0 \text{ V}$$

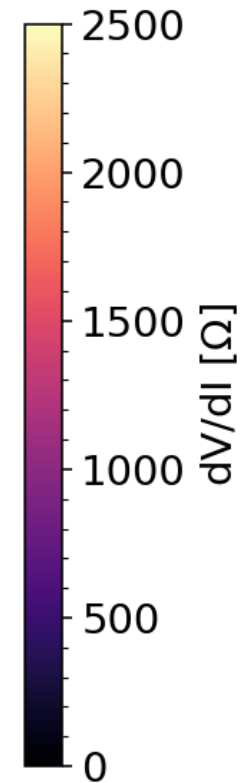
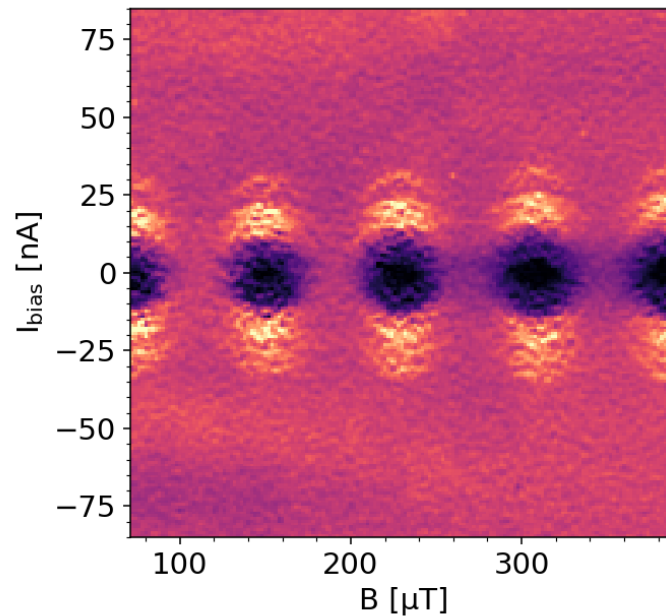


Interference vs backgate

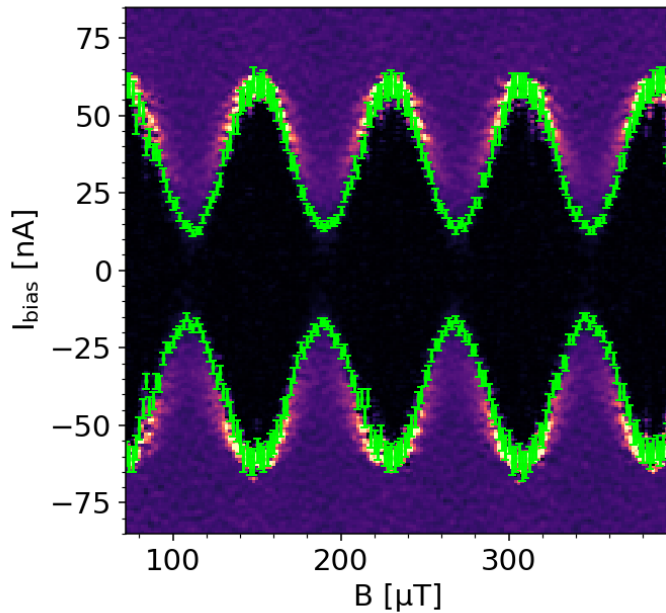
$$V_{BG} = 7.1 \text{ V}$$



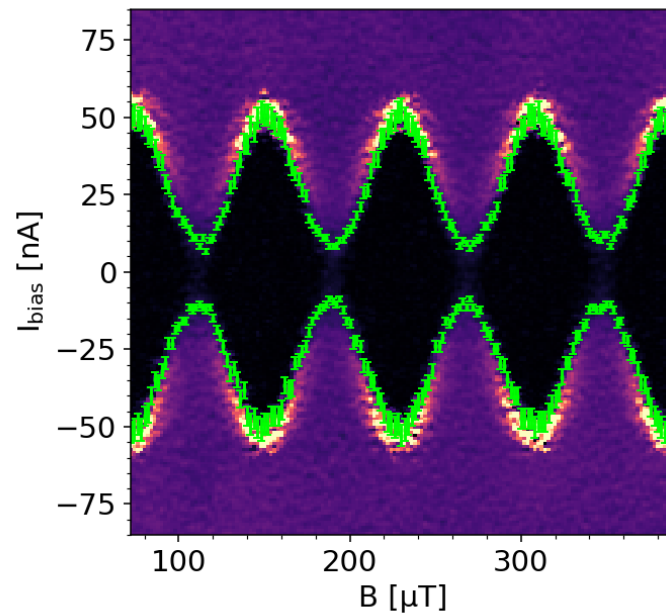
$$V_{BG} = 5.3 \text{ V}$$



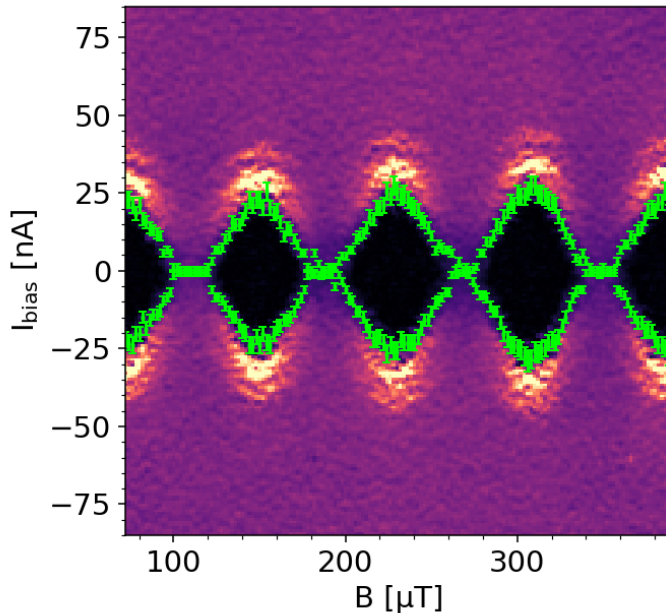
$$V_{BG} = 20.0 \text{ V}$$



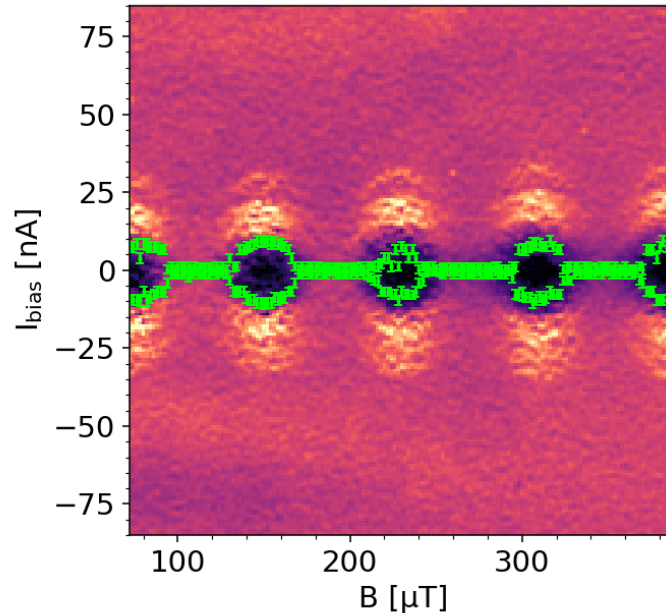
$$V_{BG} = 12.0 \text{ V}$$



$$V_{BG} = 7.1 \text{ V}$$

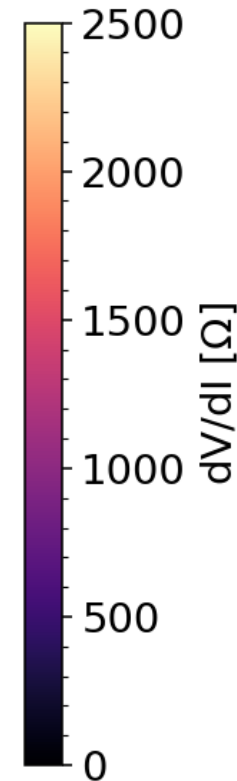


$$V_{BG} = 5.3 \text{ V}$$



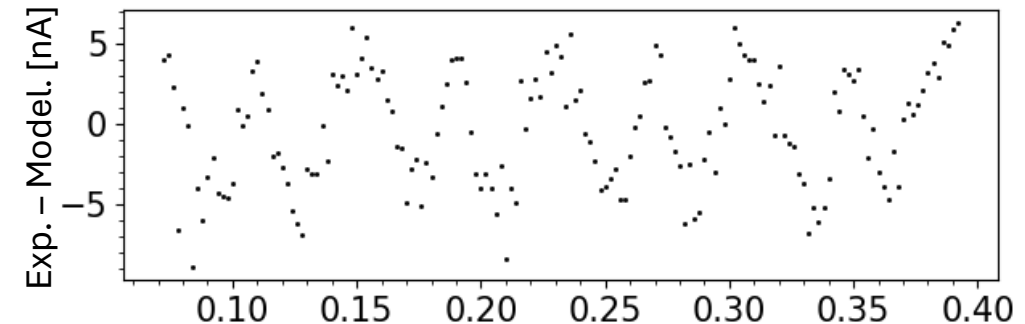
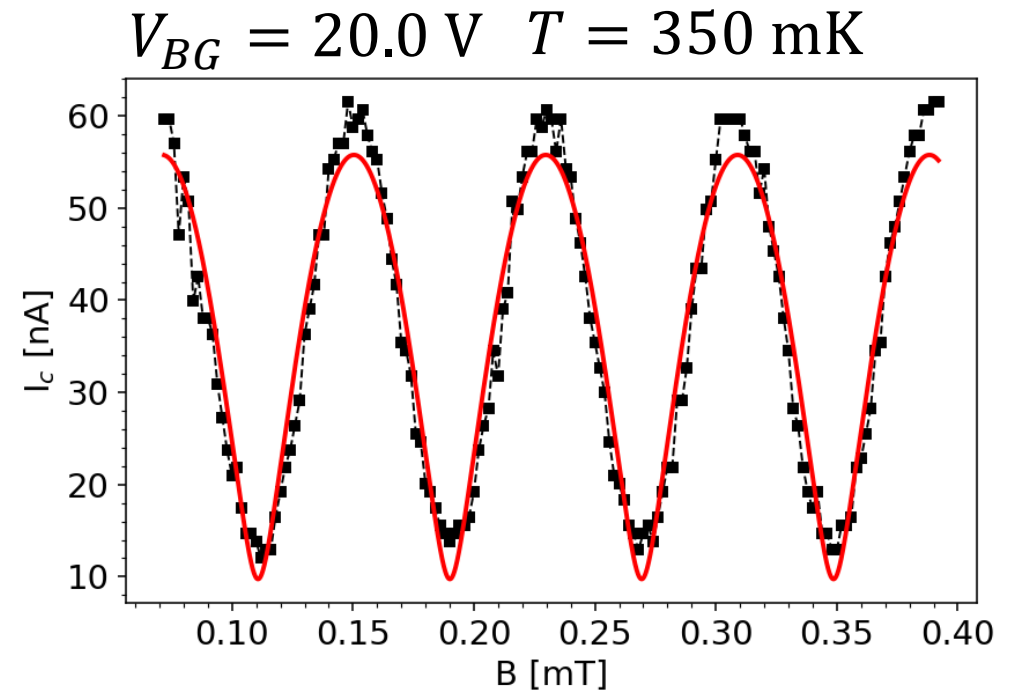
Interference vs backgate

- $T = 350 \text{ mK}$
- SQUID pattern is not symmetric for all the backgate values
→ **JJ are not identical**
- At low V_{BG} destructive interference is obtained for a range of magnetic field.



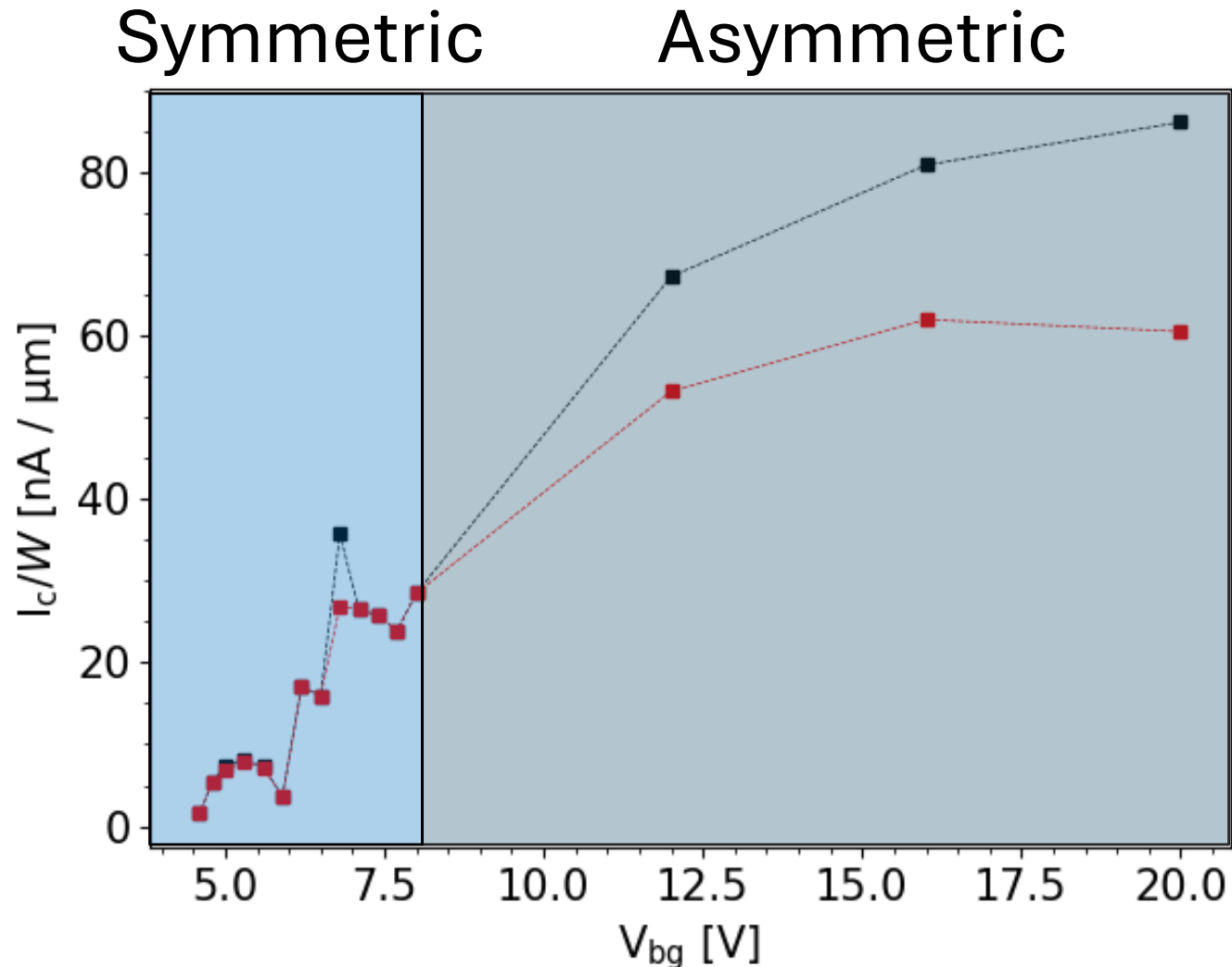
First Model

- $I_c = \sqrt{(I_{c1} - I_{c2})^2 + 4I_{c1}I_{c2} \cos\left(\pi \frac{BA}{\Phi_0} + \text{fase}\right)^2}$
- $I_{c1} = 32.8 \pm 0.4 \text{ nA}$
- $I_{c2} = 23.0 \pm 0.5 \text{ nA}$
- $A_{\text{eff}} = 26.10 \pm 0.1 \mu\text{m}^2$
- $A_{\text{geo}} = 13.6 \mu\text{m}^2$
- $\rightarrow F = 1.9$



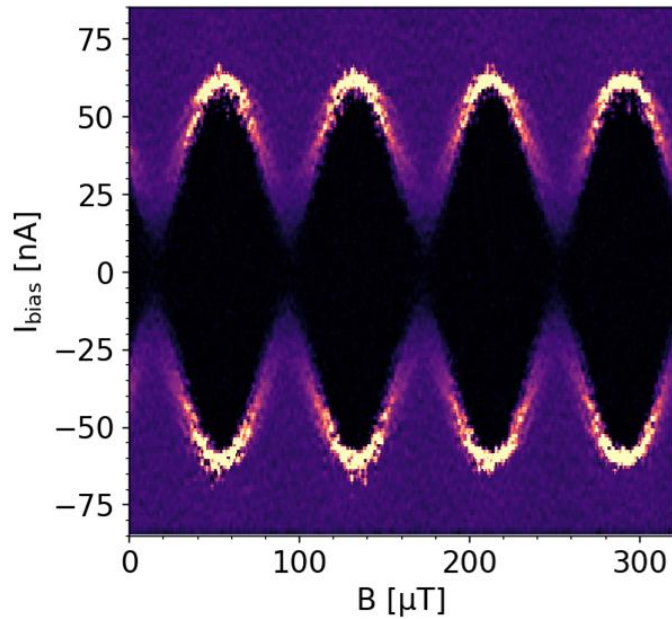
20240711/m054_a

SQUID regimes vs backgate

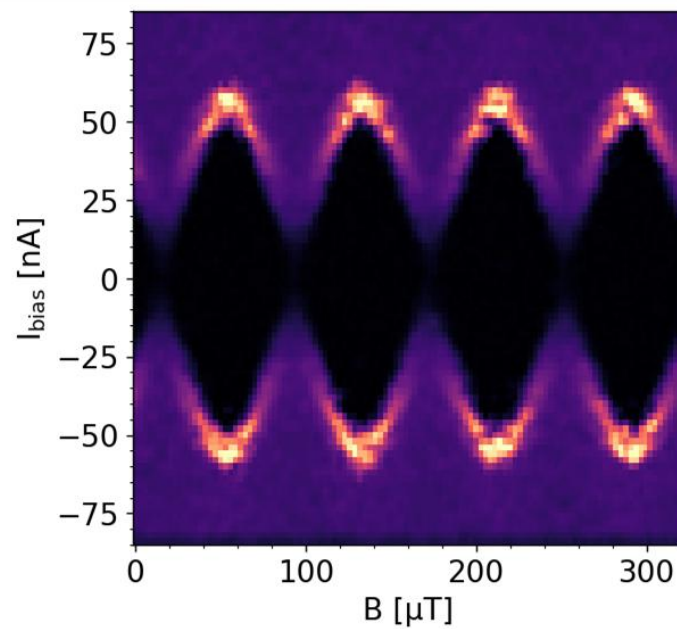


- $I_{c1}/W = 86 \text{ nA } \mu\text{m}^{-1}$
- $I_{c2}/W = 61 \text{ nA } \mu\text{m}^{-1}$
- Different effective channel lengths?
- Different interface transparency?

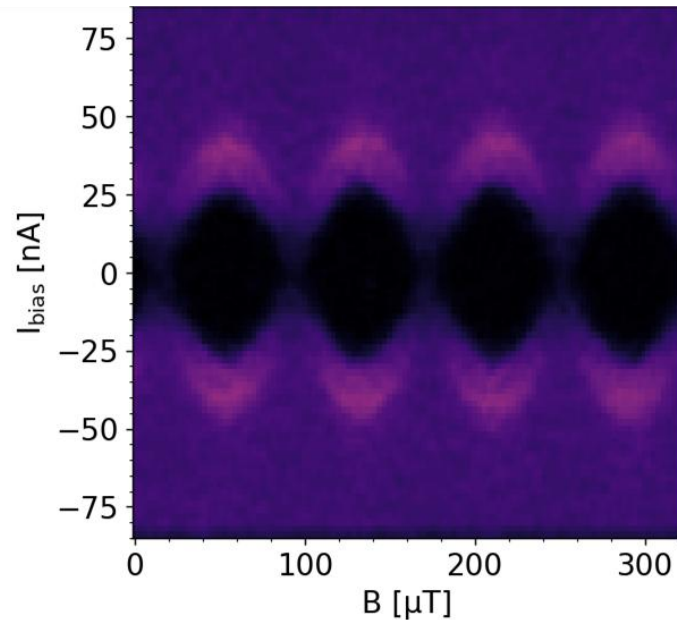
$T = 0.42\text{ K}$



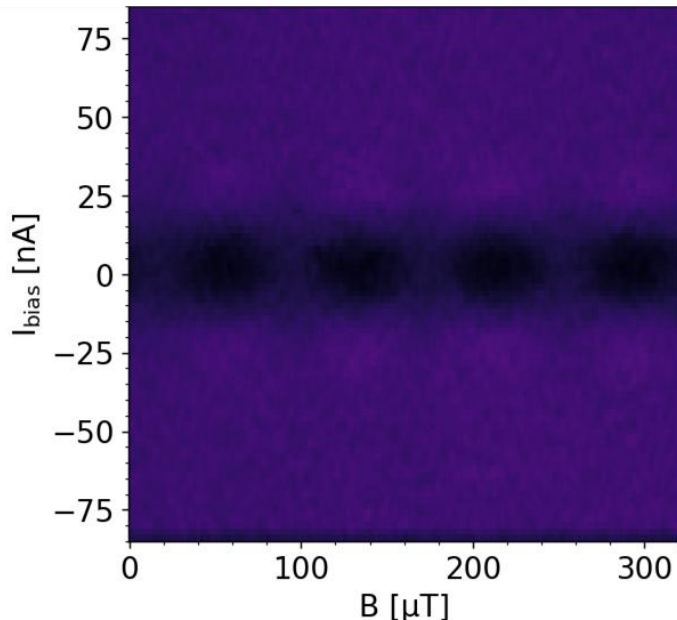
$T = 0.5\text{ K}$



$T = 0.9\text{ K}$



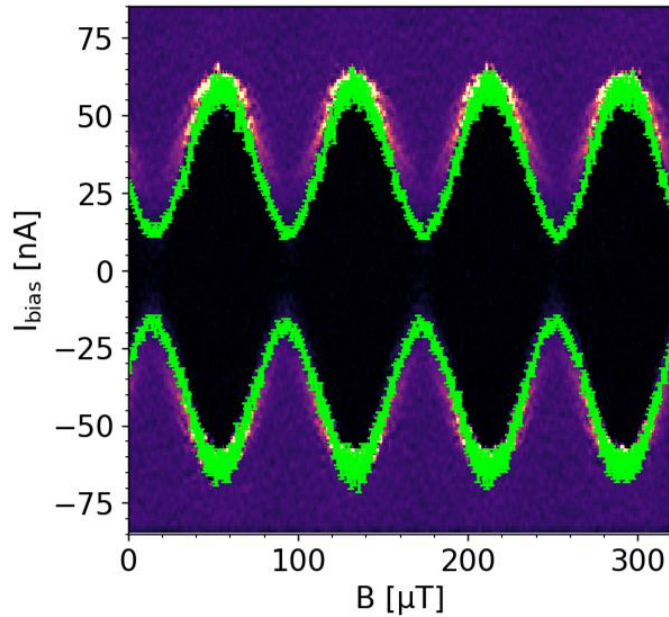
$T = 1.55\text{ K}$



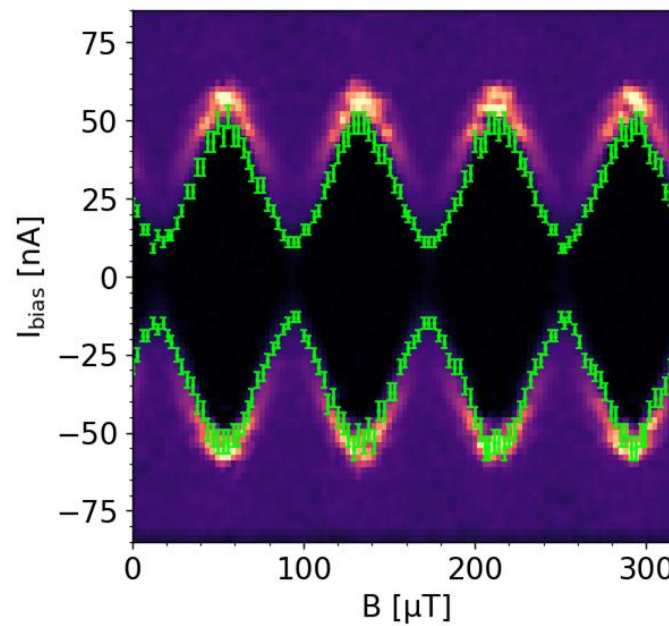
Interference vs temperature

• $V_{BG} = 20.0\text{ V}$

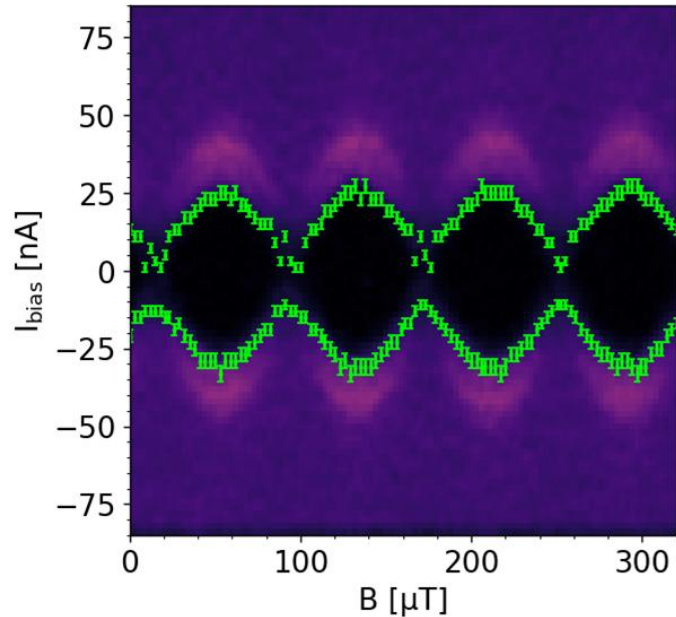
$T = 0.42\text{ K}$



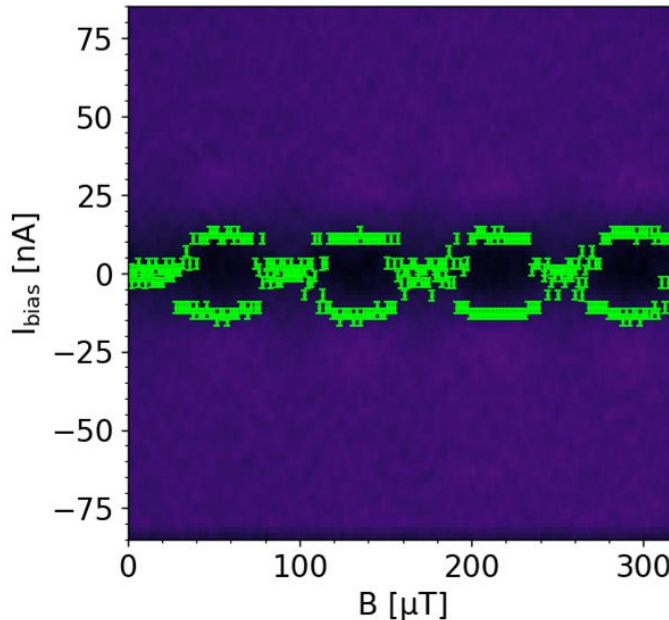
$T = 0.5\text{ K}$



$T = 0.9\text{ K}$

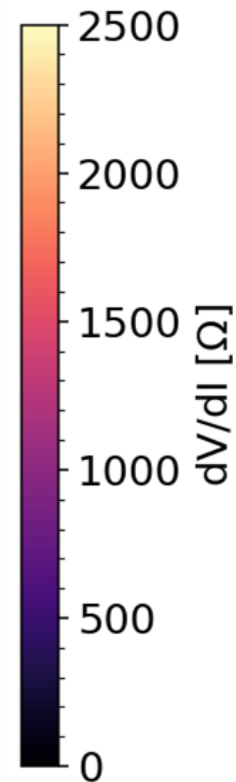


$T = 1.55\text{ K}$

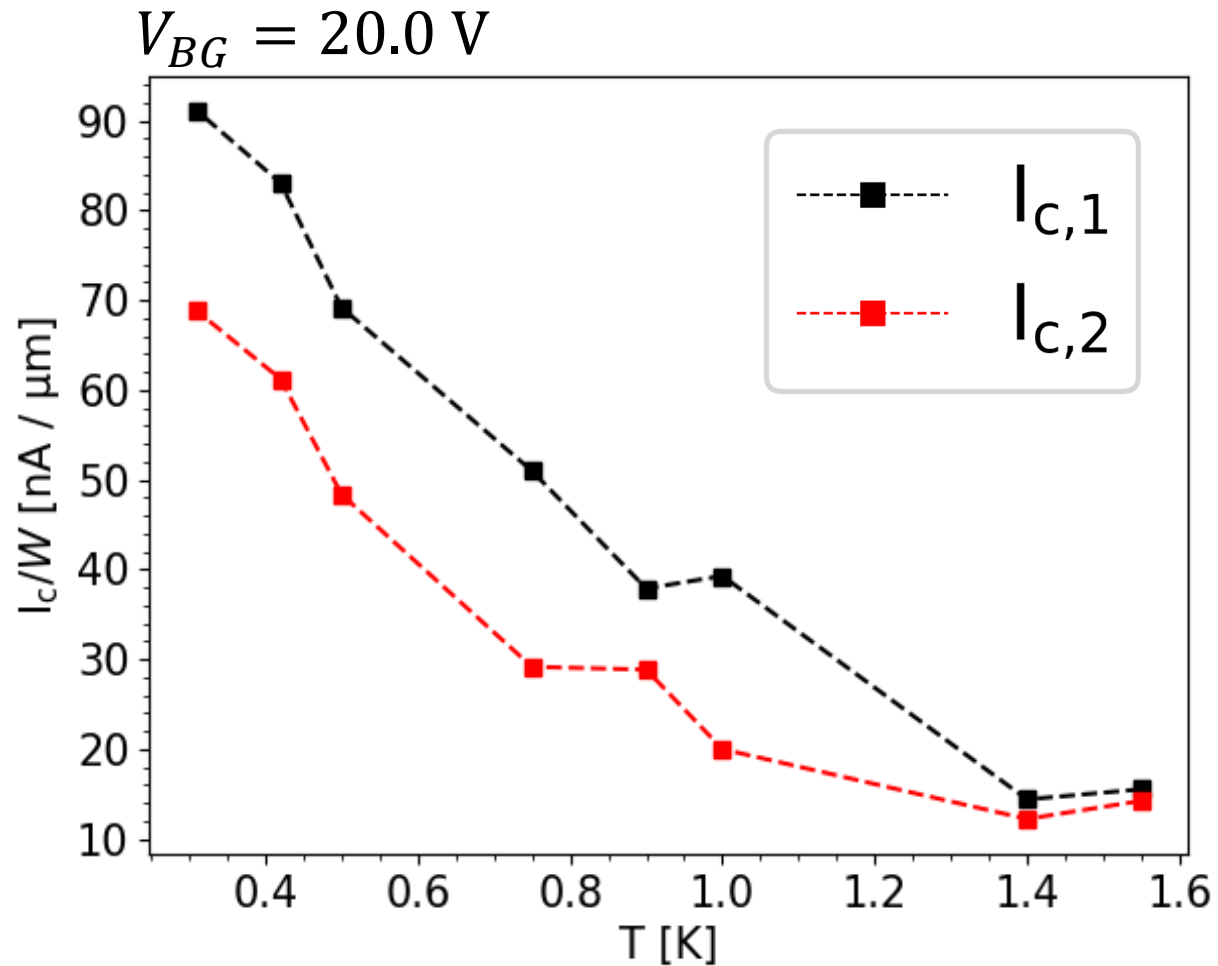


Interference vs temperature

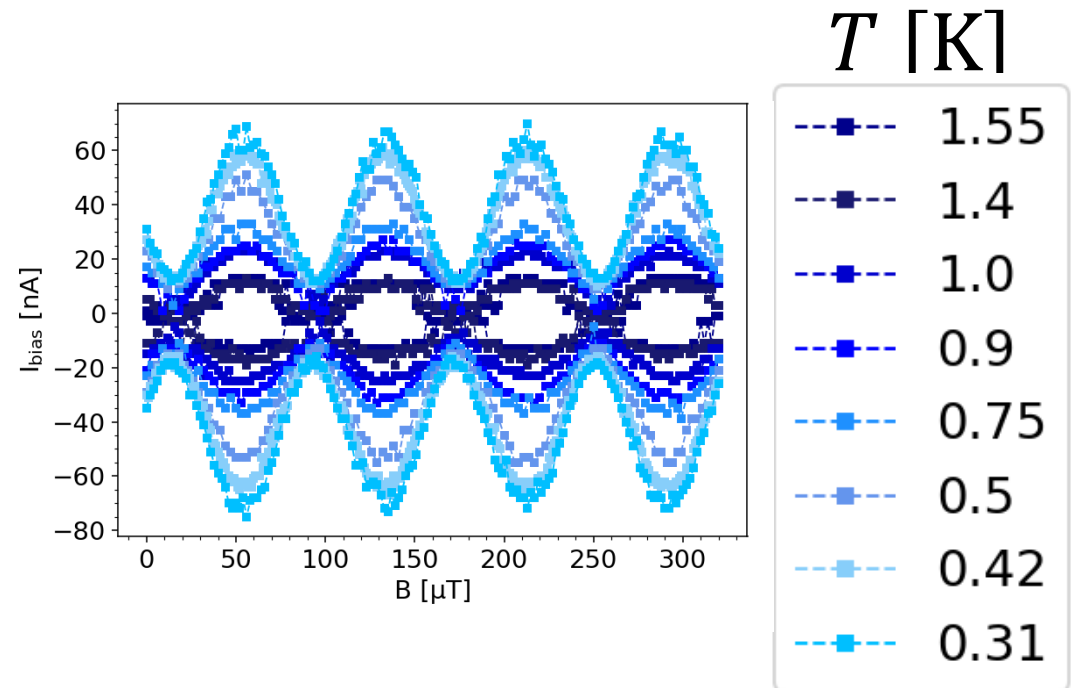
- $V_{BG} = 20.0\text{ V}$
- Asymmetry in critical currents up to 1.5 K
- If we compare with interference patterns with similar I_{c1} and I_{c2} the *shape* is different



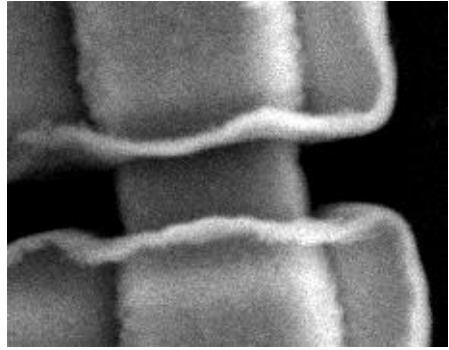
Temperature Behaviour



- Similar decay in temperature for both supercurrents.
- Slow decay above 1 K

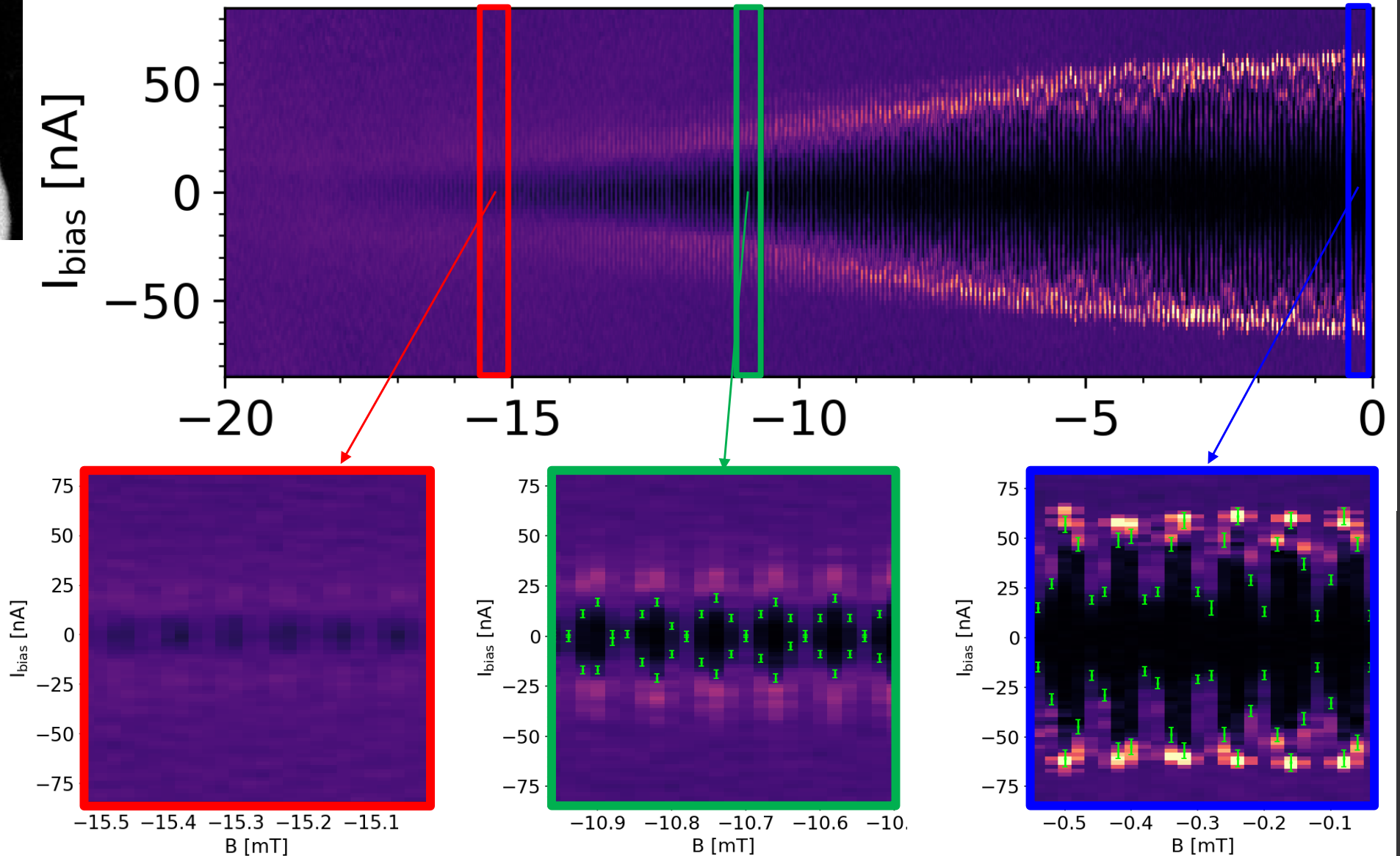


“High” magnetic field

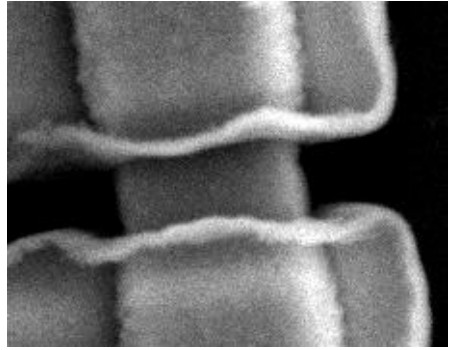


$L = 200 \text{ nm}$
 $W = 380 \text{ nm}$
 $\lambda_L = 40 \text{ nm}$

$dV/dI [\Omega]$ 0 500 1000 1500 2000 2500



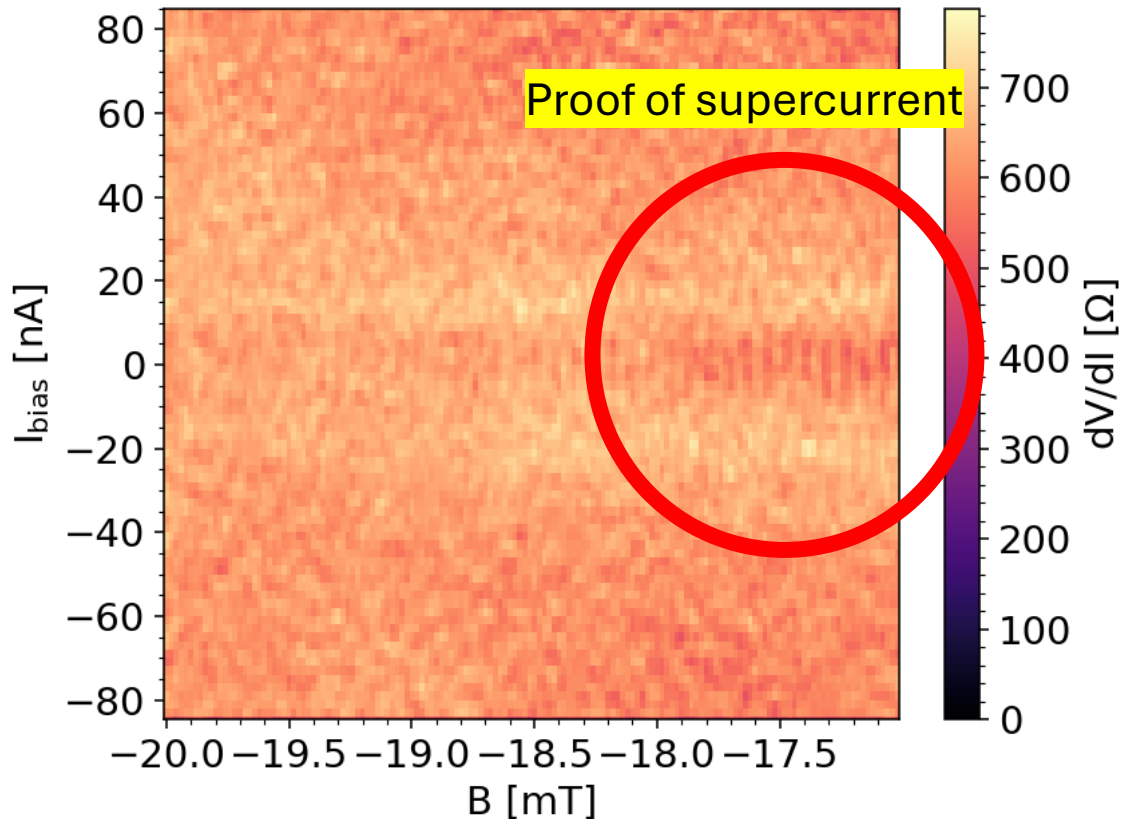
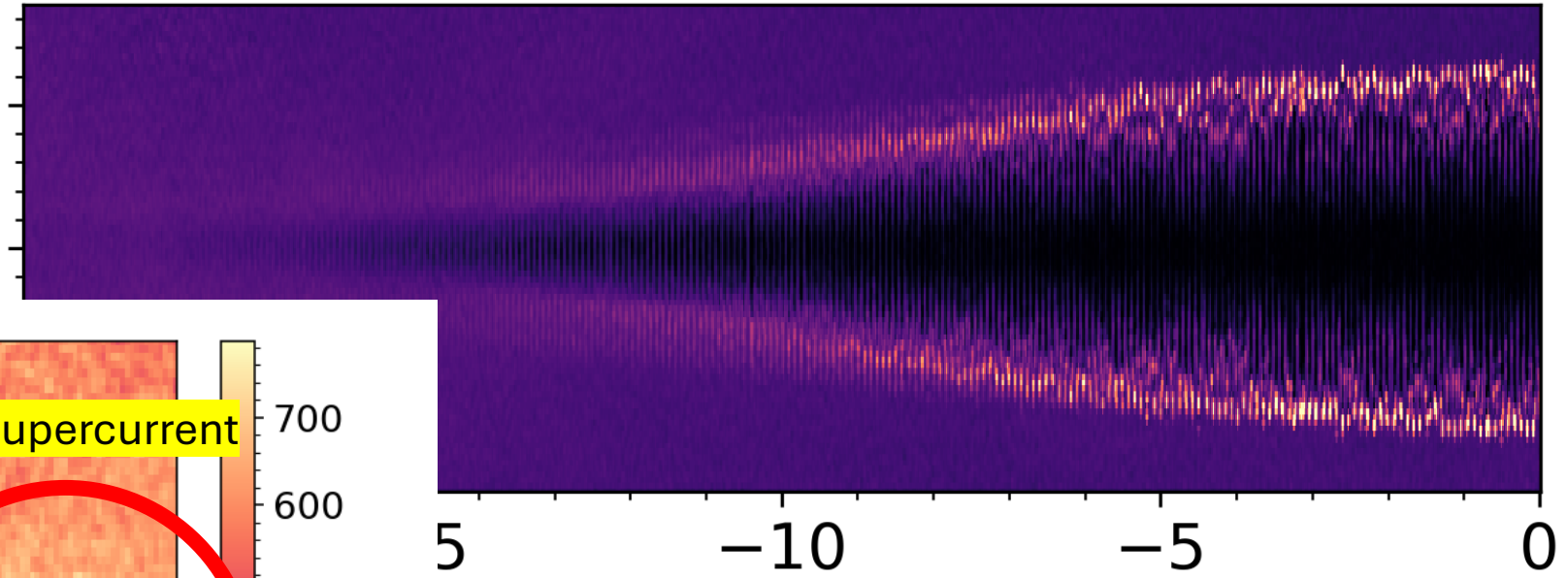
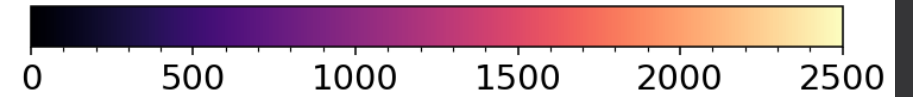
“High” magnetic field



I_s [nA]

50
0

dV/dI [Ω]



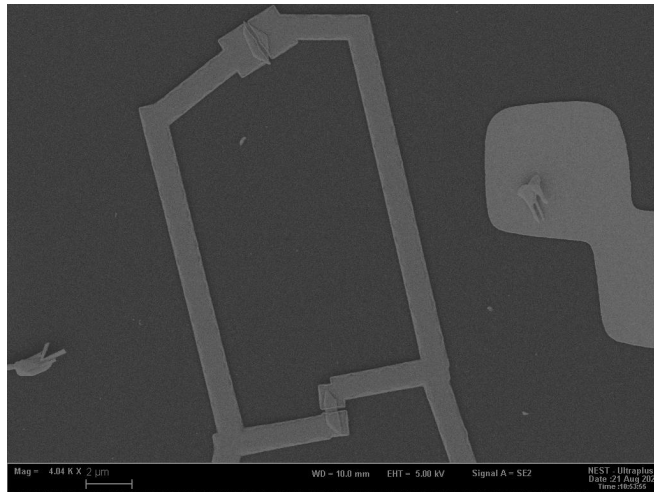
$$\Phi_0 = 2.07 \text{ mT } \mu\text{m}^2$$

$$I_c(18.5 \text{ mT}) \cong 0 \text{ nA} \rightarrow A = 0.11 \mu\text{m}^2$$

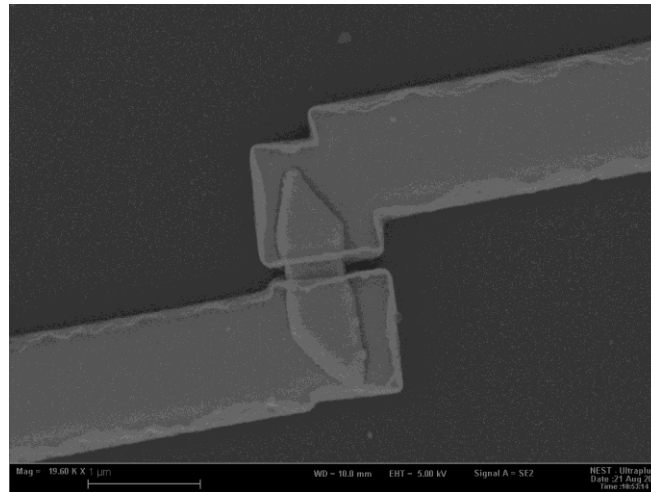
$$A_{JJ1} = (L + 2\lambda_L) \times W = 0.11 \mu\text{m}^2$$

Results Asymmetric SQUID

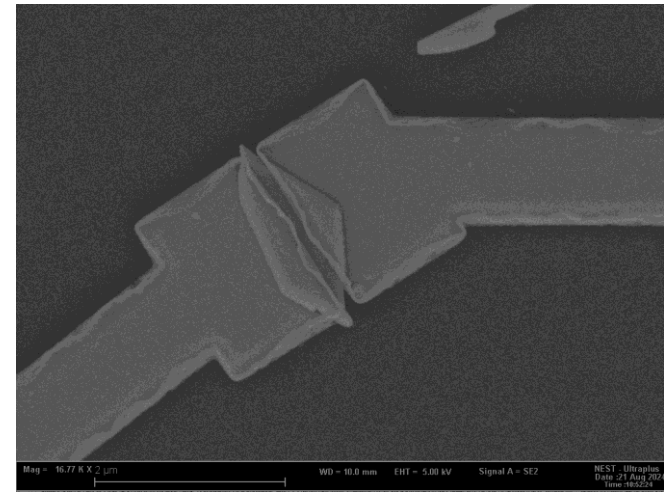
SEM: H6S4



$$A = 60 \mu\text{m}^2$$

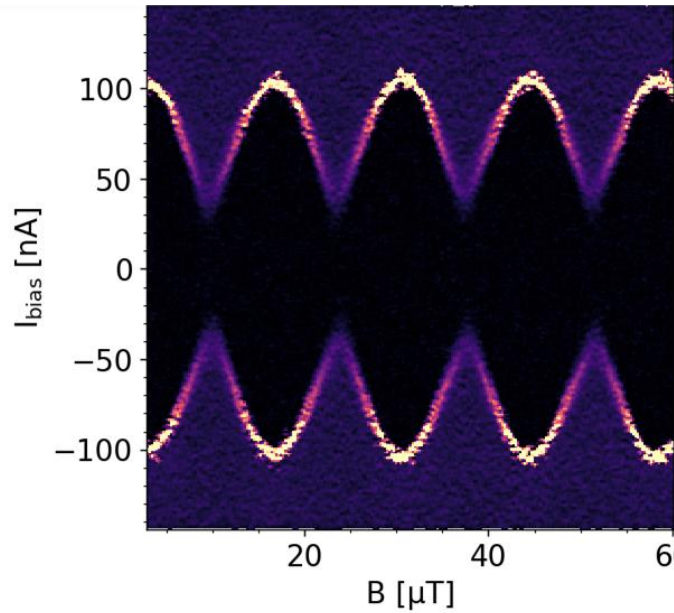


$$\begin{aligned} L &= 190 \text{ nm} \\ W &= 530 \text{ nm} \\ A &= 0.10 \mu\text{m}^2 \end{aligned}$$

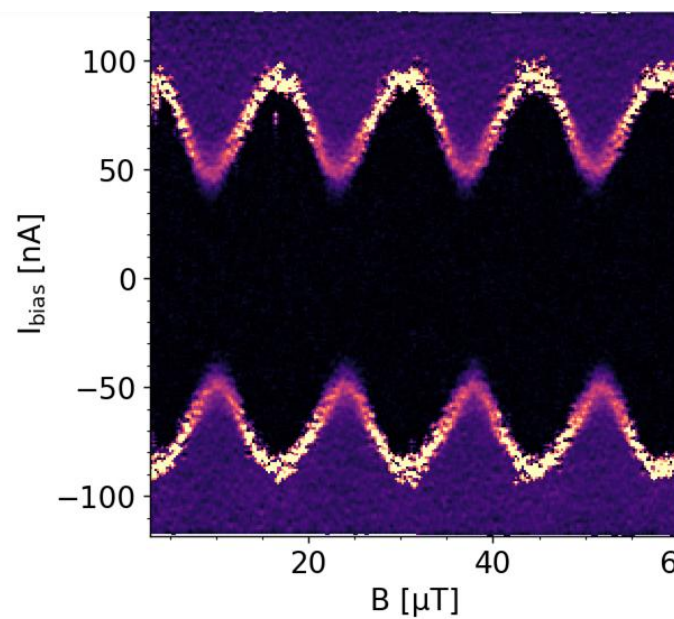


$$\begin{aligned} L &= 180 \text{ nm} \\ W &= 1.7 \mu\text{m} \\ A &= 0.30 \mu\text{m}^2 \end{aligned}$$

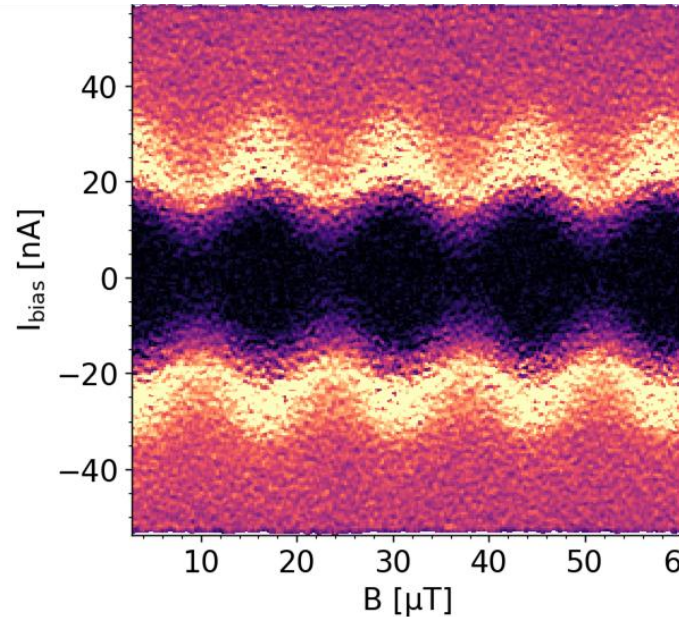
$$V_{BG} = 18.0 \text{ V}$$



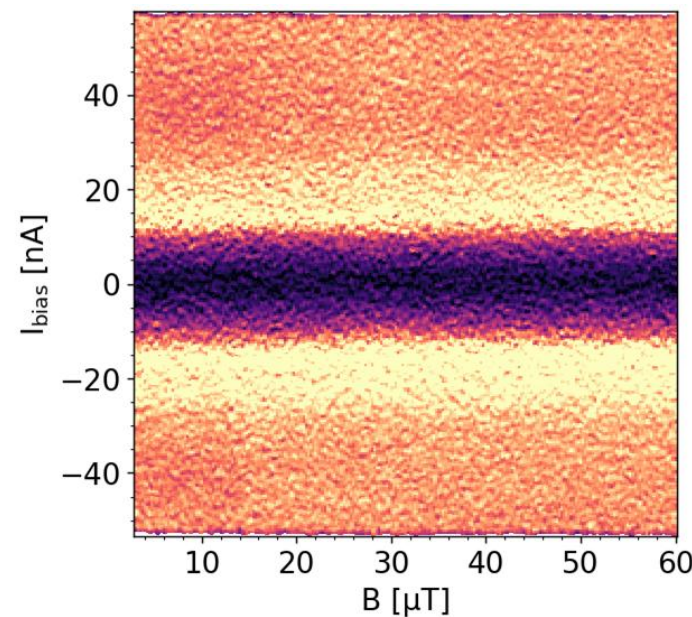
$$V_{BG} = 9.0 \text{ V}$$



$$V_{BG} = 4.5 \text{ V}$$

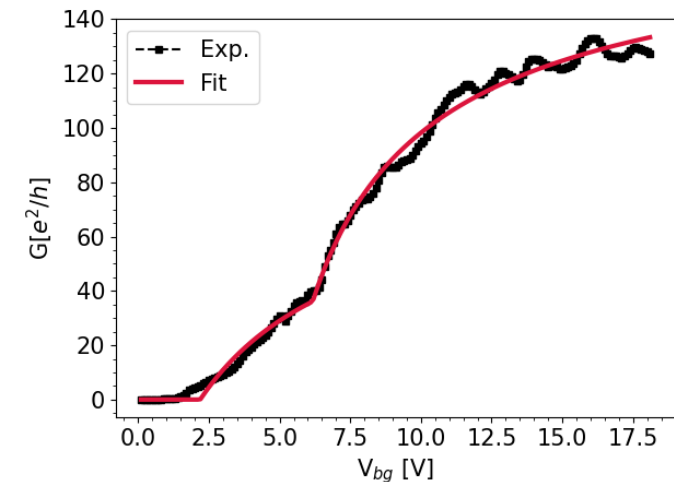
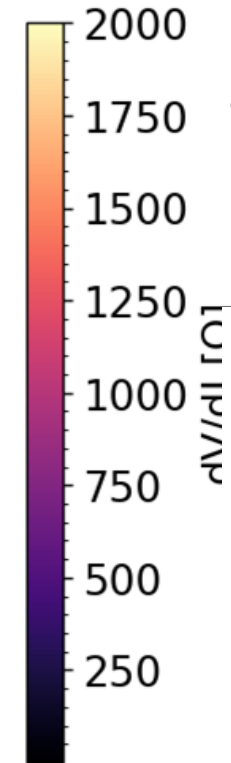


$$V_{BG} = 4.0 \text{ V}$$

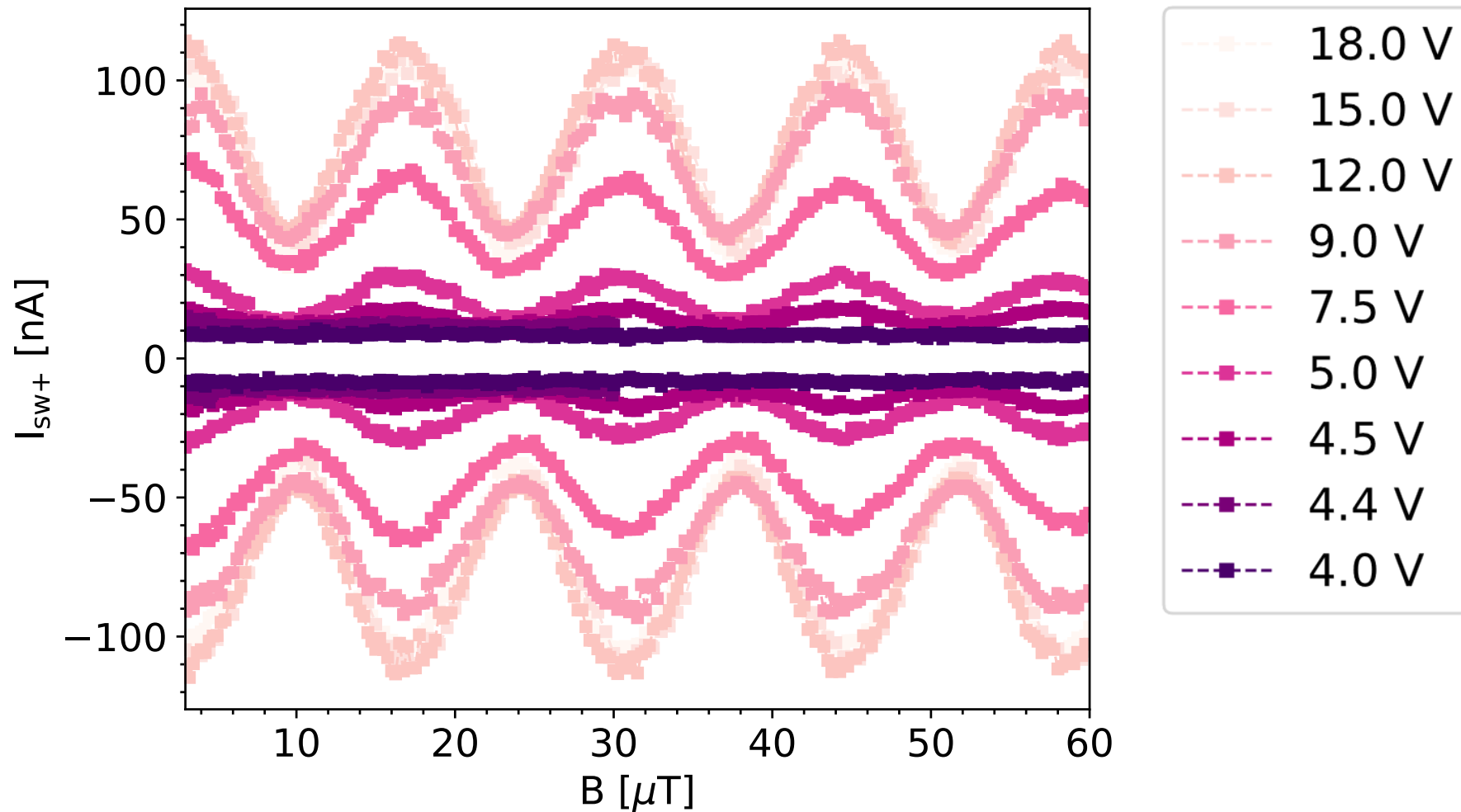


Interference vs backgate

- $T = 350 \text{ mK}$
- Always in the asymmetric regime
- Loss of interference for $V_{BG} = 4.0 \text{ V}$

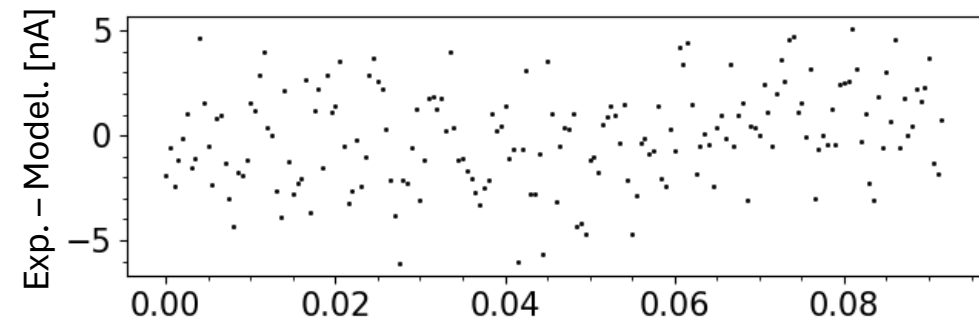
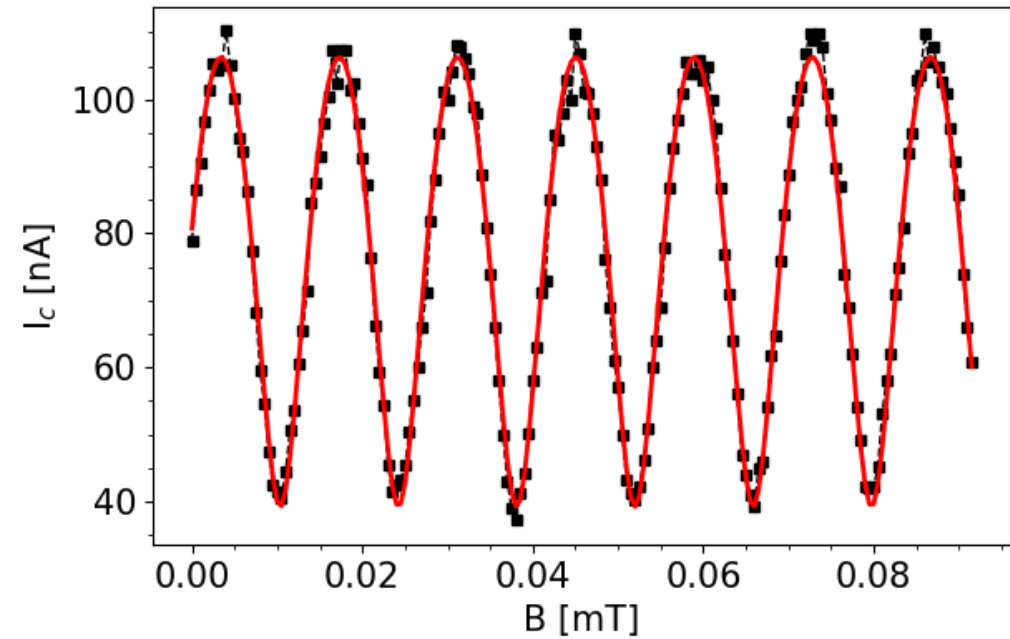


I_{sw} versus backgate

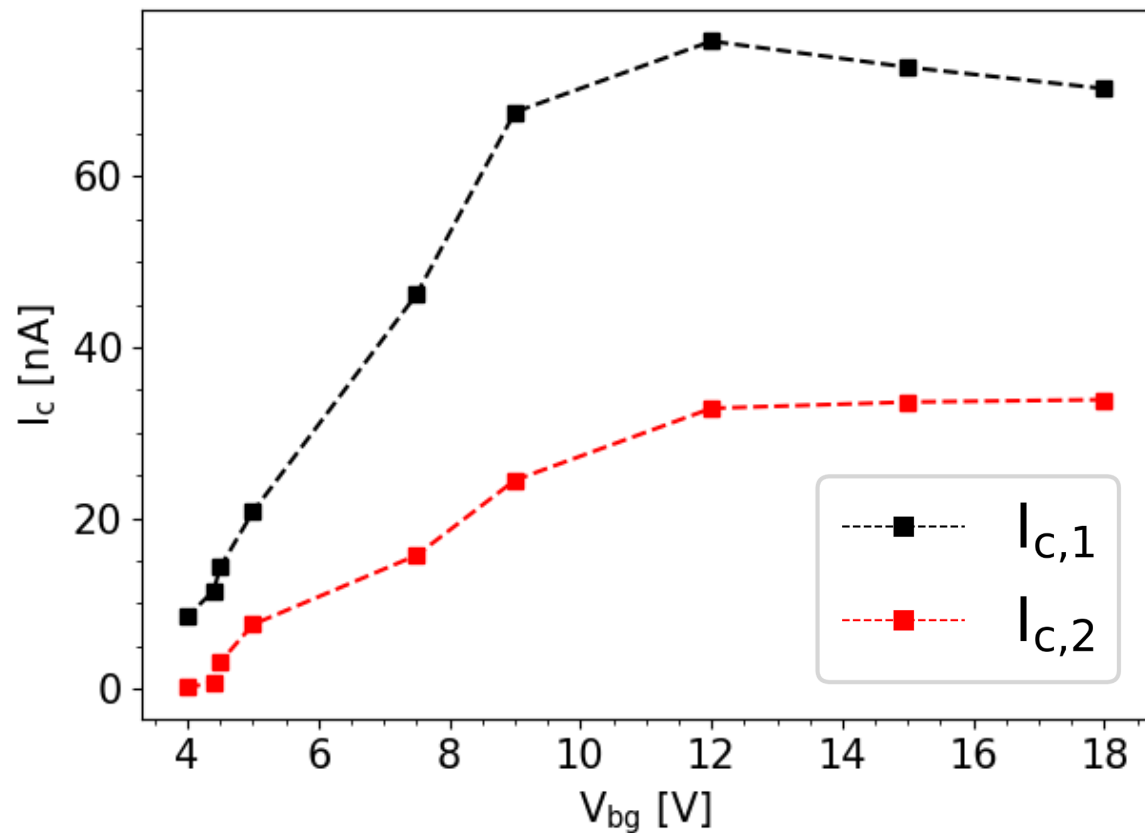


First Model

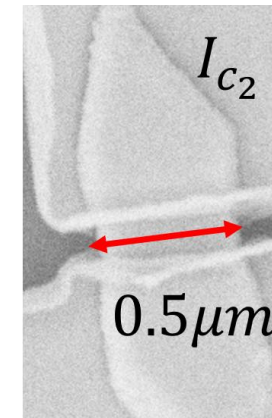
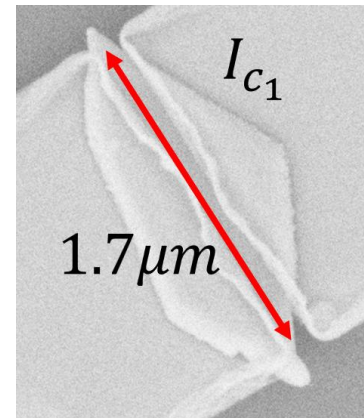
- $I_c = \sqrt{(I_{c1} - I_{c2})^2 + 4I_{c1}I_{c2} \cos\left(\pi \frac{BA}{\Phi_0} + \text{fase}\right)^2}$
- $I_{c1} = 72.8 \pm 0.2 \text{ nA}$
- $I_{c2} = 33.6 \pm 0.3 \text{ nA}$
- $A_{\text{eff}} = 149.0 \pm 0.1 \mu\text{m}^2$
- $A_{\text{geo}} = 60 \mu\text{m}^2$
- $\rightarrow F = 2.5$



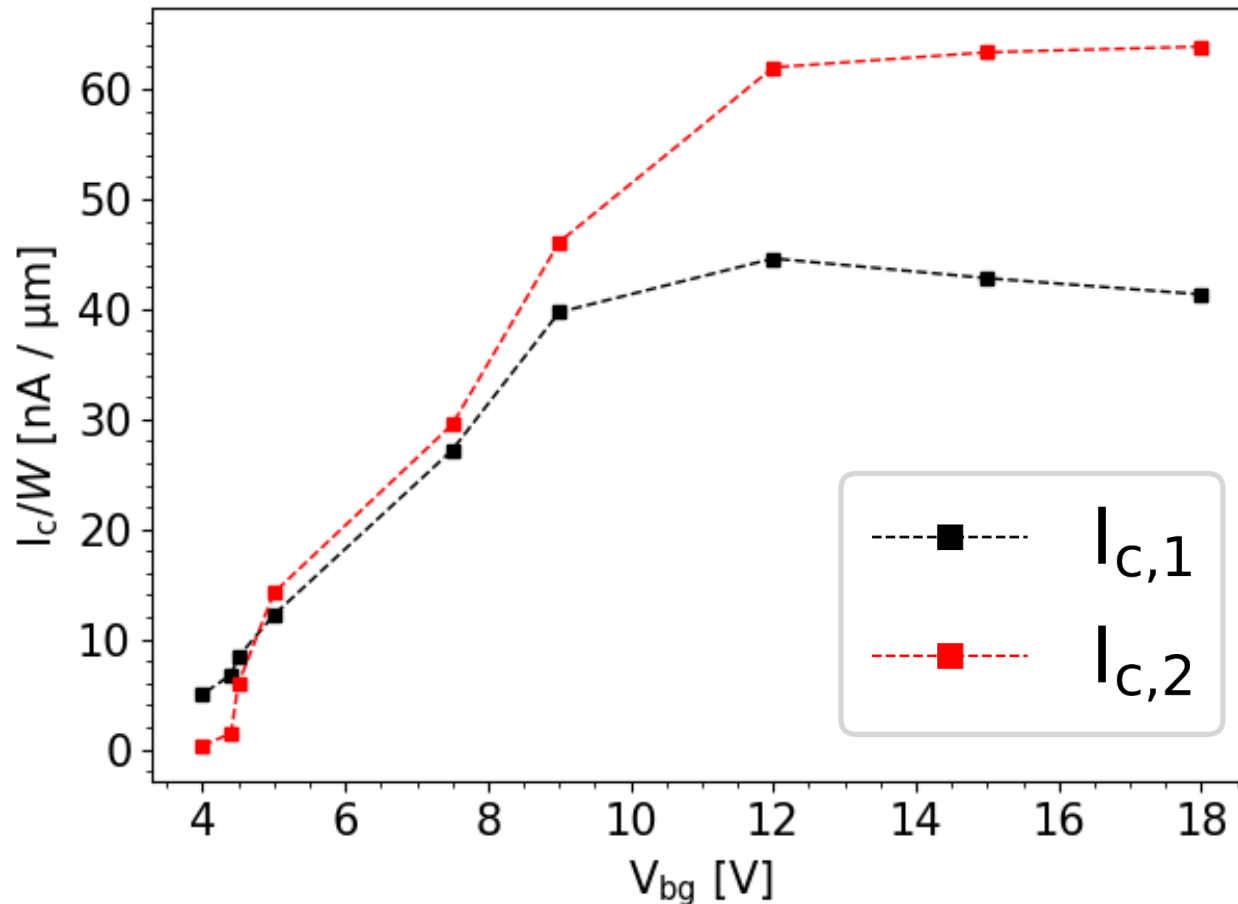
Critical Current vs backgate



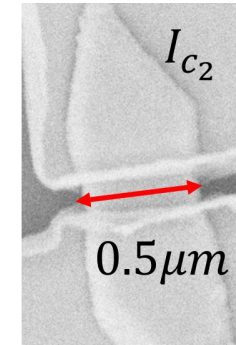
- I associate the higher critical current to the wider flag.



Critical current density versus backgate

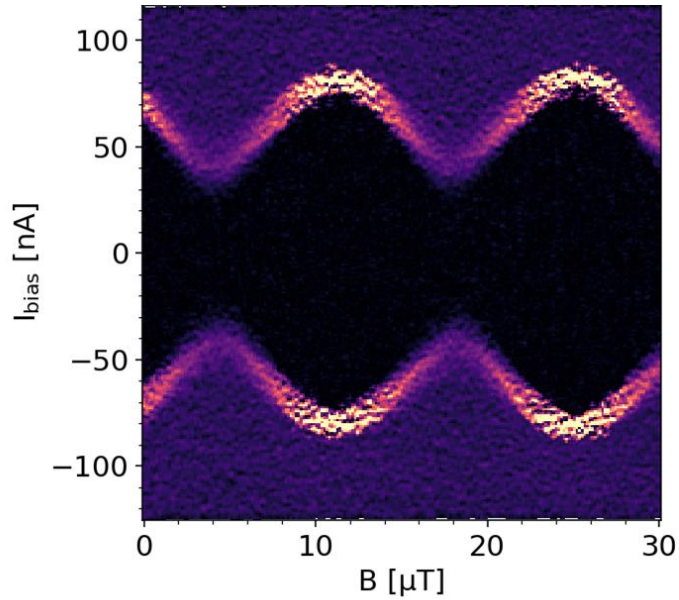


- $I_{c1}/W_1 = 40 \text{ nA } \mu\text{m}^{-1}$
- $I_{c2}/W_2 = 62 \text{ nA } \mu\text{m}^{-1}$
- The narrow flag has higher supercurrent density
- The narrow flag is the one that show pinch off at $V_{BG} = 4.0 \text{ V}$

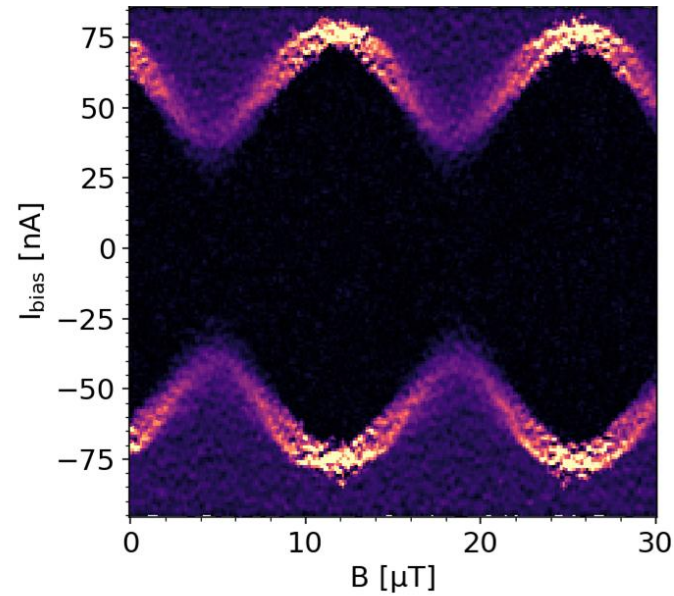


- $I_{c1}/W_1 = 40 \text{ nA } \mu\text{m}^{-1}$
- $I_{c2}/W_2 = 62 \text{ nA } \mu\text{m}^{-1}$
- The narrow flag has higher supercurrent density
- The narrow flag is the one that show pinch off at $V_{BG} = 4.0 \text{ V}$

$T = 0.42\text{ K}$

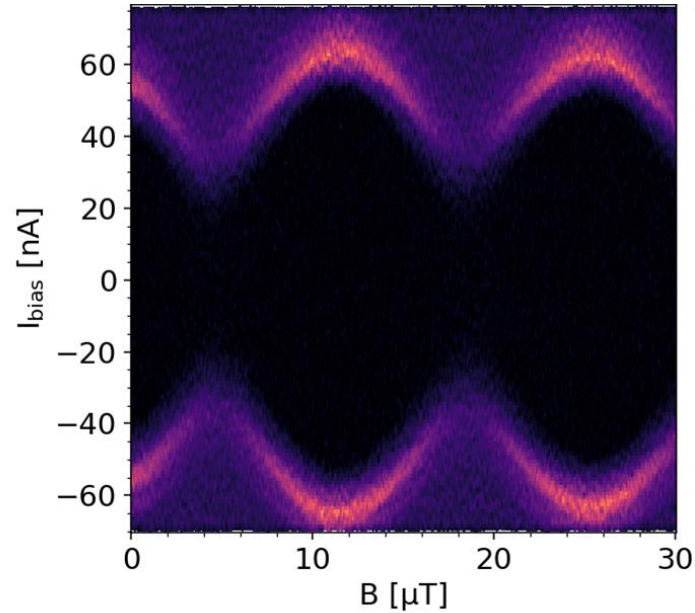


$T = 0.55\text{ K}$

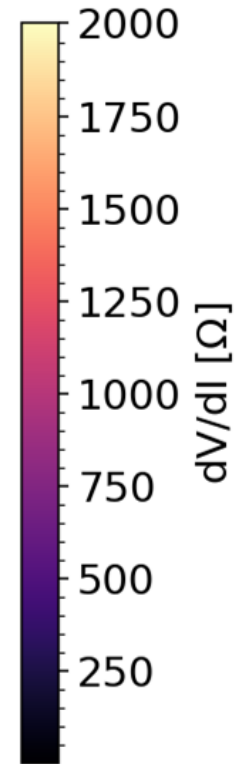
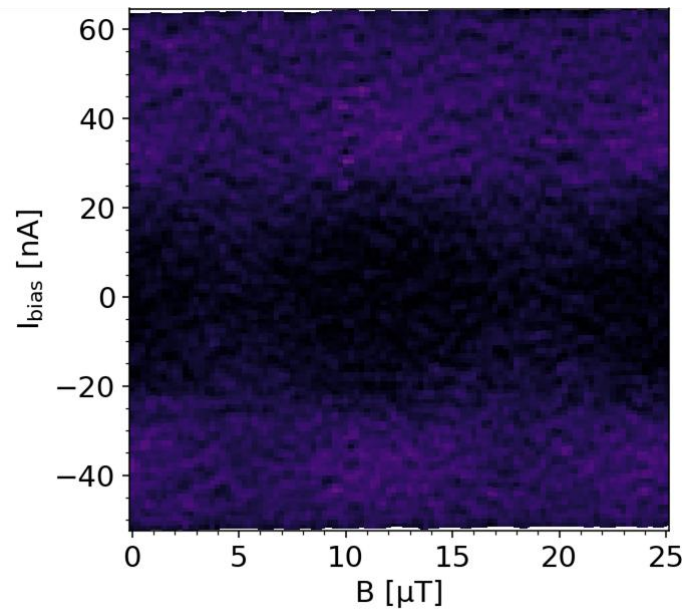


Interference vs temperature

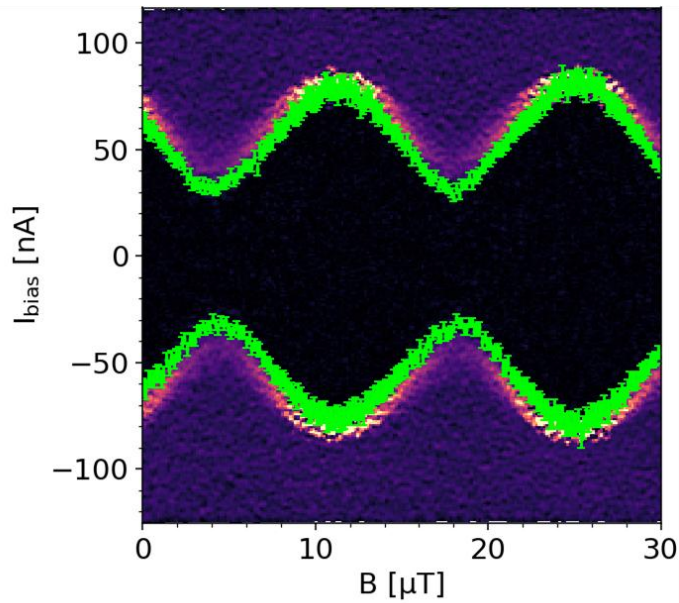
$T = 0.8\text{ K}$



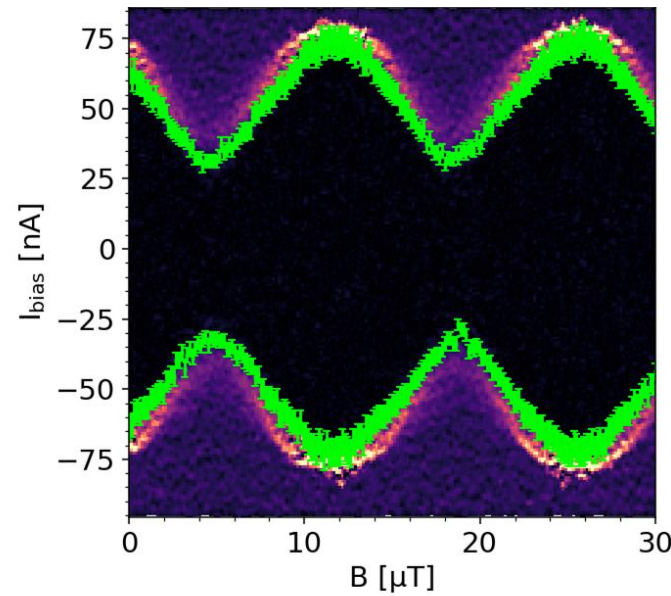
$T = 1.5\text{ K}$



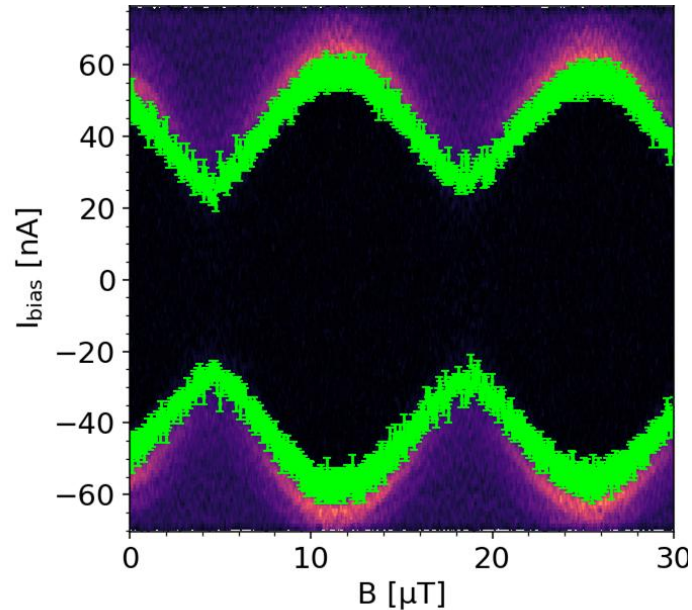
$T = 0.42\text{ K}$



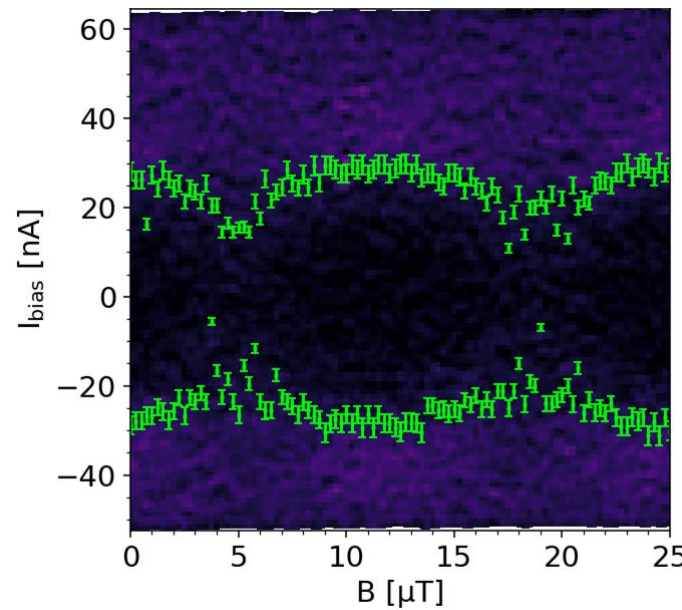
$T = 0.55\text{ K}$



$T = 0.8\text{ K}$

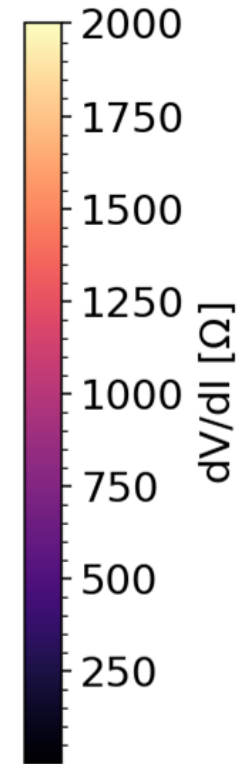


$T = 1.5\text{ K}$

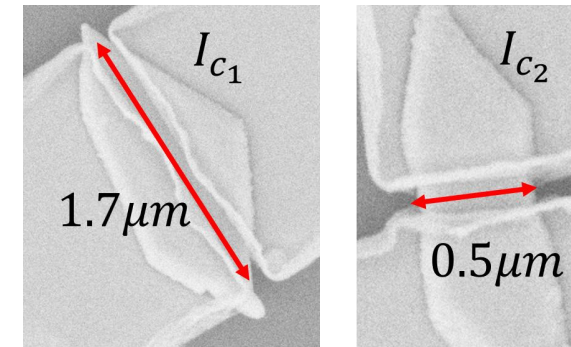


Interference vs temperature

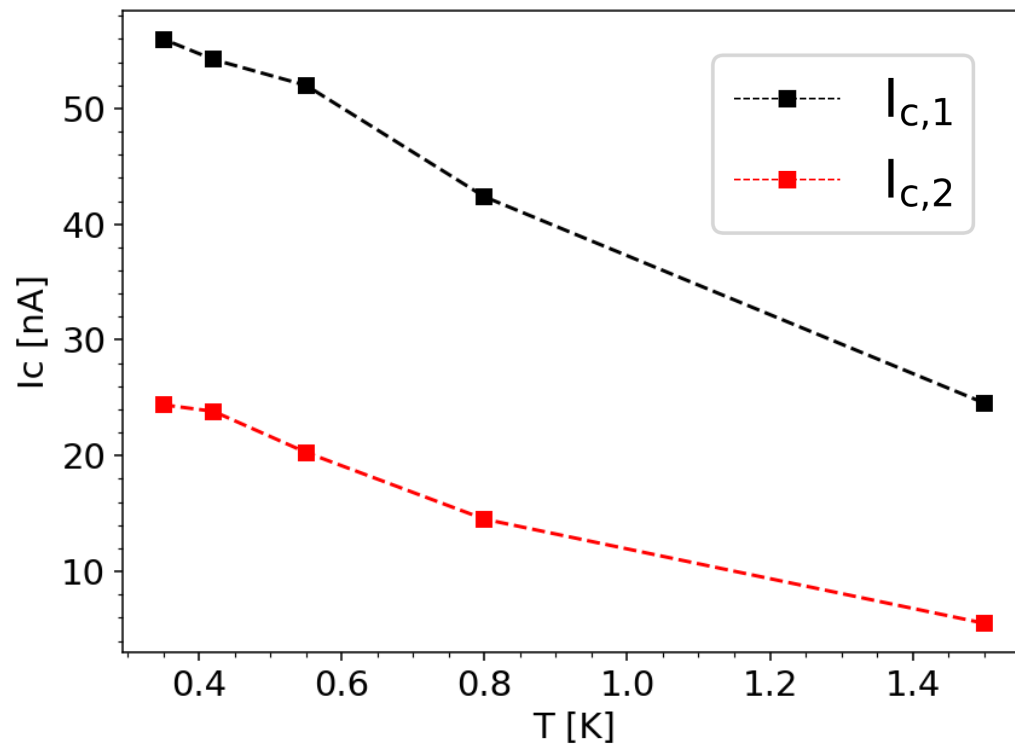
- Interference is visible also at 1.5 K



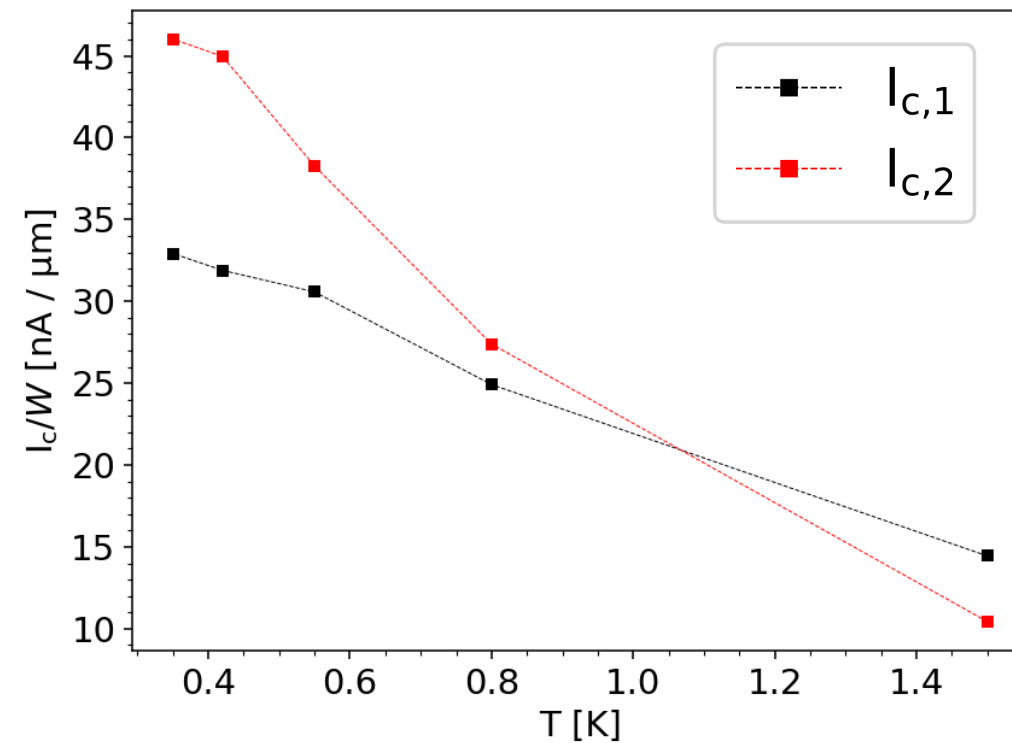
Critical Currents vs temperature



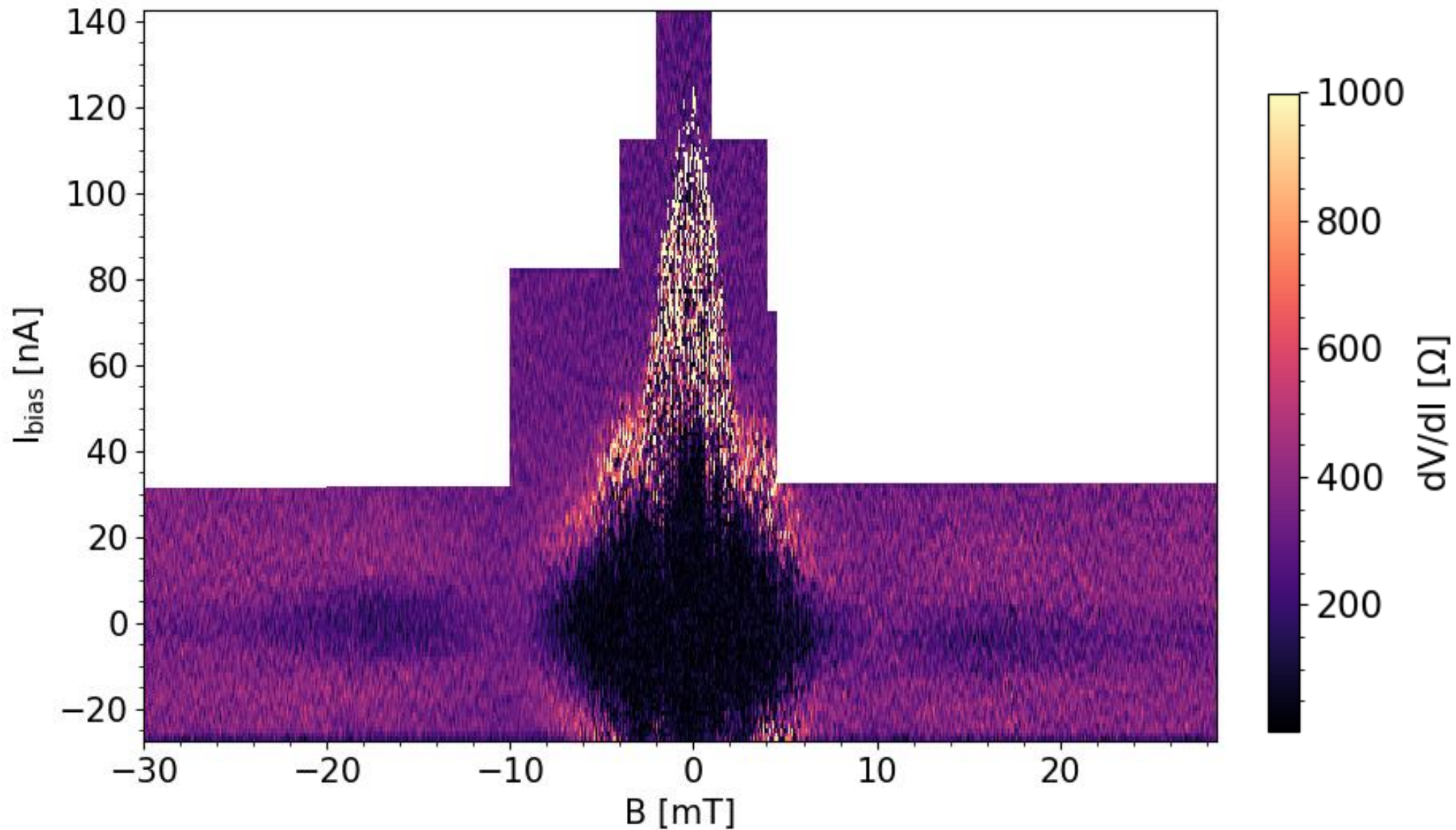
Critical Current



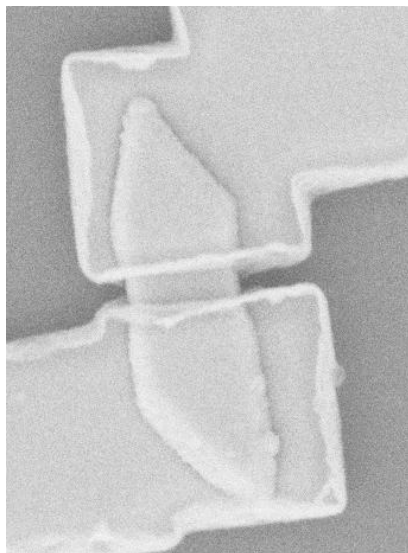
Critical Current Density



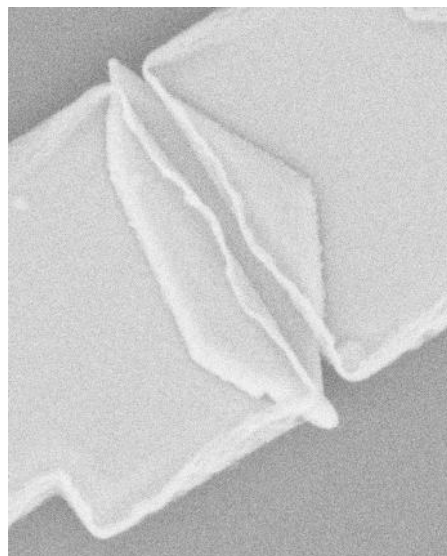
“High” Magnetic Field



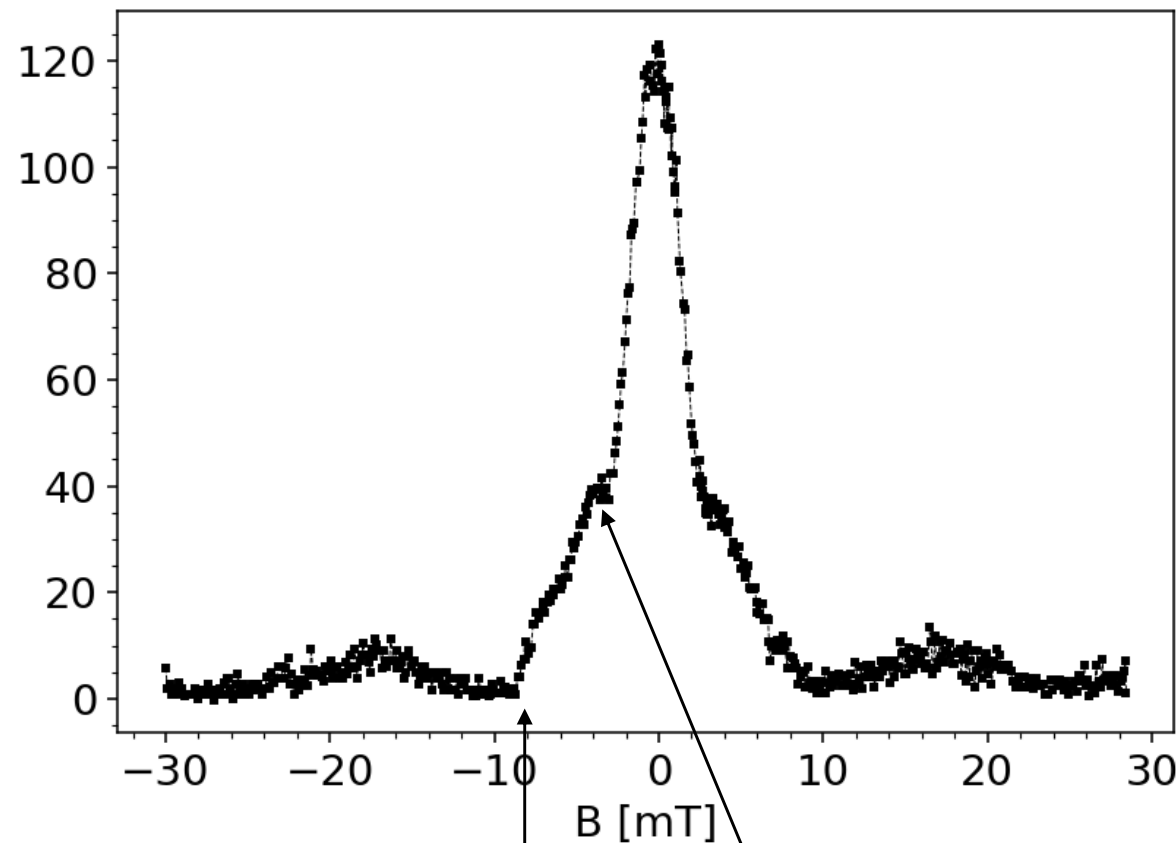
Fraunhofer Envelope



$$A = 0.14 \mu\text{m}^2$$



$$A = 0.44 \mu\text{m}^2$$



$$A = 0.20 \mu\text{m}^2$$

$$A = 0.61 \mu\text{m}^2$$

Conclusions

- SQUID-type interference on InSb Nanoflags has been demonstrated.
- Backgate controlled destructive interference properties in the symmetric SQUID.
- Backgate was able to extinguish interference in the asymmetric SQUID

Thanks for your attention!